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Abstract: We compare some dynamic scheduling heuristics that have shown good performances on simulation study against MCT on experiments on real solving platforms. The heuristics rely on a prediction module, the Historical Trace Manager. They have been implemented in NetSolve, a Problem Solver Environment built on the client-agent-server model. Numerous different scenarios have been examined and many metrics have been considered. We show that the predicting module allows a better precision in task duration estimation and that our heuristics optimize several metrics at the same time while outperforming MCT.

Key-words: time-shared resources, dynamic scheduling heuristics, historical trace manager, MCT, client-agent-server

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Comparaison et étude du comportement d'heuristiques basées sur l'enregistrement de l'historique des tâches dans un système client-agent-serveur

Résumé : Des expériences de simulation nous ont montré que certaines de nos heuristiques étaient à même de donner de bons résultats sur une plate-forme réelle. Ces heuristiques reposent sur un module de prédiction de la durée des tâches, le gestionnaire de l'historique des tâches (HTM). Nous avons implanté nos heuristiques et le HTM dans le code de NetSolve, un environement de résolution de problèmes utilisant le modèle client-agent-server. NetSolve utilise MCT, une heuristique réputée pour sa facilité d'implantantion et ses bons résultats, comme heuristique d'ordonnancement par défaut. Dans ce travail, nous comparons nos heuristiques à MCT sur dix scénarios différents et leurs performances sont analysées sur plusieurs métriques. Les résultats valident l'utilisation du HTM ainsi que nos heuristiques, qui donnent d'importants gains par rapport à MCT sur plusieurs métriques à la fois.

Mots-clés : ressources temps partagées, heuristiques dynamiques d'ordonnancement, gestionnaire d'historique des tâches, MCT, client-agent-serveur

1. Introduction

GridRPC [NMS+03] is an emerging standard promoted by the global grid forum (GGF)[1]. This standard defines both an API and an architecture. A GridRPC architecture is heterogeneous and composed of three parts: a set of clients, a set of servers and an agent (also called a registry). The agent has in charge to map a client request to a server. In order for a GridRPC system to be efficient, the mapping function must choose a server that fulfills several criteria. First, the total execution time of the client application, e.g. the makespan, has to be as short as possible. Second, each request of every clients must be served as fast as possible. Finally, the resource utilization must be optimized.

Several middlewares instantiate the GridRPC model (NetSolve [CD96], Ninf [NSS99], DIET [CDF+01], etc.). In these systems, a server executes each request as soon as it has been received: it never delays the start of the execution. In this case, we say that the execution is *time-shared* (in opposition to *space-shared* when a server executes at most one task at a given moment). In NetSolve, the scheduling module uses MCT (Minimum Completion Time) [MAS+99] to schedule requests on the servers. MCT was designed for scheduling an application for space-shared servers. The goal was to minimize the makespan of a set of independent tasks. This leads to the following drawbacks:

- *mono-criteria and mono-client*. MCT was designed to minimize the makespan of an application. It is not able to give a schedule that optimizes other criteria such as the response time of each request. Furthermore, optimizing the last task completion date does not lead to minimize each client application makespan. However, in the context of GridRPC, the agent has to schedule requests from more than one client.
- *load balancing*. MCT tries to minimize the execution time of the last request. This leads to over-use the fastest servers. In a time-shared environments, this implies to delay previously mapped tasks and therefore degrades the response time of the corresponding requests.

Furthermore, MCT requires sensors that give information on the system state. It is mandatory to know the network and servers state in order to take good scheduling decisions. However, supervising the environment is intrusive and disturbs it. Moreover, the information are sent back from time to time to the agent: they can be out of date when the scheduling decision is taken.

In order to tackle these drawbacks we propose and study three scheduling heuristics designed for GridRPC systems. Our approach is based on a prediction module embedded in the agent. This module is called the Historical Trace Manager (HTM) and it records all scheduling decisions. It is not intrusive and since it runs on the agent there is no delay between the determination of the state and its availability. The HTM takes into account that servers run under the time-shared model and is able to predict the duration of a given task on a given server as well as its impact on already mapped tasks. The proposed heuristics use the HTM to schedule the tasks. We have plugged the HTM and our heuristics in the NetSolve system and performed intensive series of tests on a real distributed platform (more than 50 days of continuous computations) for various experiments with several clients.

In this paper, we compare our heuristics against MCT which is implemented by default in NetSolve on several criteria (Makespan, response time, quality of service). Results show that the proposed heuristics outperform MCT on at least two of the three criteria with gain up to 20% for the makespan and 60% for the average response time.

2. Models

The heuristics proposed in section 4 are conceived and studied for GridRPC environments [NMS+03]. They focus on shared resources, aiming at better exploiting and less perturbing the potentially loaded system. These notions are explained in this section.

[1] `http://www.ggf.org`

task	arrival date	size of the matrix	real completion date	simulated completion date	difference	percentage of error
1	33.00	1500	80.79	79.99	0.8	1.7
2	59.92	1200	92.08	93.19	-1.11	3.4
3	73.92	1800	142.79	142.50	0.29	0.4
1	29.41	1500	76.69	76.29	0.4	0.8
2	56.43	1200	89.15	89.50	-0.35	1
4	96.41	1200	136.97	139.40	-2.43	5.9
6	140.41	1200	204.84	204.85	-0.01	0.02
3	70.42	1800	210.61	195.74	14.87	10.6
5	121.43	1500	235.38	232.92	2.46	2.2
8	181.45	1200	248.02	248.56	-0.54	0.8
9	206.41	1200	259.91	261.63	-1.72	3.2
7	166.42	1800	289.08	288.91	0.17	0.1

Table 1. Two independent task sets executions

2.1. GridRPC Model

Some middlewares are available for common use and designed to provide network access to remote computational resources for solving computationally intense scientific problems. Some of them, like NetSolve [CD96], Ninf [NSS99] and DIET [CDF+01], rely on the GridRPC model.

Recently, a standardization of Remote Procedure Call for GRID environments has been proposed [2]. This standardization defines an API and a model. The model is composed of three parts: clients which need some resources to solve numerous problems, servers which run on machines that have resources to share and an agent that contains the scheduler and maps the requested problems of clients to the available servers. Each machine of such a system can be on a local or geographically distributed heterogeneous computing network.

The submission mechanism works as follows: the client requests the agent for a server that can compute its job. The agent sends back the identity of the server that scores the optimum.

In order to score each server, the scheduler needs the most accurate information on both the problem and the servers (static information) as well as on the system state (dynamic information). Static information concern each server (network and CPU peak performances) and problem descriptions (size of input and output data as well as the task cost: number of operations requested to perform the problem). Dynamic information concern each server (current CPU load, current bandwidth and latency of the network).

2.2. Information Model

In order to select the '*best*' available server, the scheduler which is embedded in the agent needs accurate information on the problem and on the servers (static information) as well as on the system state (dynamic information).

Static information concern each server (CPU and network peak performances) and problem descriptions (size of input and output data as well as the task cost: number of operations requested to perform the problem).

Dynamic information concern each server (current CPU load average, current bandwidth and latency between the agent and the server). They are computed by monitors. A NetSolve server runs its own monitors. The agent relies on the information sent by the server but may also use monitors beforehand installed such as those of

[2] `https://forge.gridforum.org/projects/gridrpc-wg/document/GridRPC_EndUser_16dec03/en/1`

NWS [WSH99].

Then, the scheduler determines the server where to allocate the new task. In NetSolve, the communication time is computed by dividing the size of the data by the bandwidth and adding the latency. The computation time is evaluated by dividing the task cost by the fraction of the currently available CPU speed. Thus, estimations are computed assuming that the state of the environment stays constant during the execution of the request.

2.3. Shared Resources Model

At a given moment it is possible that a server has to run more than one job. This happens, for instance, when the system is heavily loaded or when the set of servers is heterogeneous (in that case, for performance reasons, even if it depends on the scheduling policy, the agent will be very likely to often select the fastest servers). This is true even if servers are dedicated to the grid middleware.

We consider a simple but realistic model. When a server executes n tasks, each task is given $1/n$ of the total power of the resource. This model does not take into account the priorities of tasks (each task is supposed to have the same importance). We have experimented this model on LINUX and SOLARIS systems when tasks are matrix multiplications and have the same priorities. Two examples are given in Table 1. Tasks are ranked by their completion date. We give for each task the percentage of error between the estimation and the real *duration* of the task. It is defined by 100 multiplied by the absolute value of the difference divided by the real duration of the task).

We have designed a *historical trace manager* (HTM) that stores and keeps track of information about each task. It simulates the execution of tasks on resources and is able to predict the completion time of each task assigned to a server. It is used by our scheduling heuristics.

In order to make the estimations, the HTM performs a discrete simulation of the execution of each task. The HTM can therefore build or update the Gantt chart for each server when a new incoming task is mapped as it is presented in Figure 1. The agent disposes of the Gantt chart given on the top of the figure. Two tasks have been scheduled on the server and a new one arrives at time $t = a_3$. The agent simulates its execution. Therefore, the three tasks share the processor capacity and each one receives 33.3% until time T_1 where the first task finishes. Then, task 2 and task 3 receives 50% of the server CPU.

Using the HTM information leads to accurate prediction of the finishing time of the tasks assigned to a server, but the heuristics which have all those information can also consider the *perturbation* tasks have on each other, and consequently envisage other metrics than the common makespan on which to score the servers. When assigning a new task, the HTM does not consider that the load of the server is constant to the one at the arrival date of the new task all along its duration. Then, the information of the new or updated Gantt charts are used by the agent to schedule tasks more accurately to optimize the chosen metric.

The simulation of the distributed environment is done for each three parts of the tasks: input data transfer, computing phase and output data transfer.

Usefulness of the HTM Here follows an example that shows how the Historical Trace Manager can help in taking good scheduling decisions:

Let us suppose that the set of servers is made up of two identical servers (same network capabilities, same CPU peak speed, same set of problems, etc.). At time 0, the client sends to these servers two tasks T_1 and T_2, whose durations on each server is 100 and 1000 seconds respectively, with no input data. Let the agent schedule T_1 on the server 1 and T_2 on the server 2 for example. At time 80, let a client request the agent to schedule a task T_3 whose duration is 100 seconds.

Without the historical trace manager, the agent knows only that server 1 and server 2 have the same load and therefore is not able to decide which is the best server to schedule T_3 (in practice, as there are dynamic information

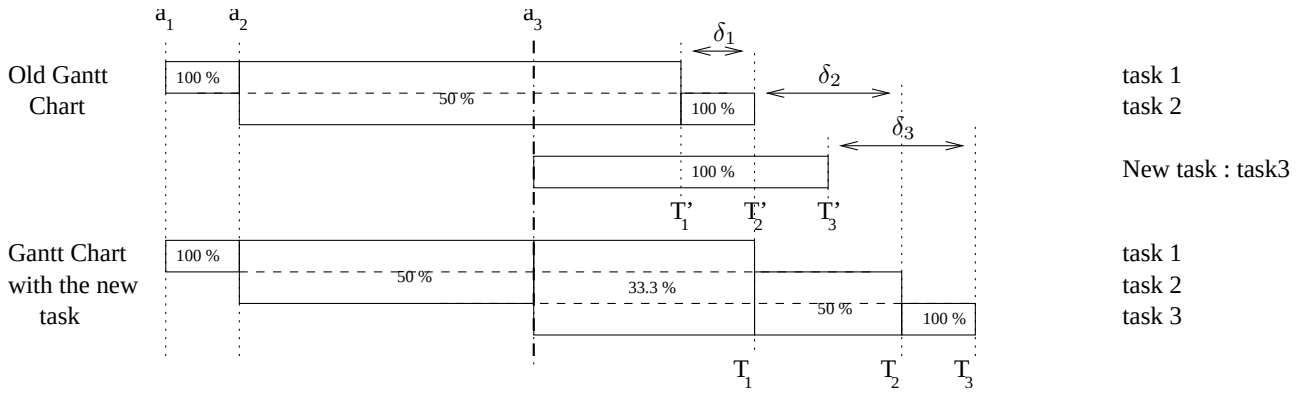

Figure 1. Notations for the historical trace use

and as the evolution of the load average is not necessarily exactly the same on the two machines, the decision is somewhat blurred).

However, the HTM simulates the execution of tasks on each server and the agent knows that the remaining duration of task T_1 is 20 seconds while the remaining duration of task T_2 is 920 seconds, therefore it knows that scheduling T_3 on server 1 will lead to a shorter completion time than scheduling T_3 on server 2.

2.4. Notations

We use the same notation in the rest of the paper than in the HTM (see Fig 1): a_i is the arrival date of task i. T_i' is the simulated finishing date in the current system state and C_i is the real one (*post-mortem*). The HTM can simulate the execution of a new task n and give the new simulated completion dates T_i of all tasks i, for all $i \leq n$. We define for all $k \leq n$, $\delta_k = T_k - T_k'$, the *perturbation* the task n produces on each running ones. We also define for all $k \leq n$, $D_k = T_k - a_n$, the *remaining* duration of the task k before completion. $p(i)$ is the server where the task i is mapped and d_i its duration on the unloaded server.

3. Metrics

In current grid middlewares, the default scheduling heuristic implemented in the agent is often *MCT* (Minimum completion time, see [MAS+99]) or an equivalent. This heuristic is designed to minimize the makespan, i.e. the completion date of the entire application submitted to the agent. The heuristics employed in our tests are not specifically designed to only minimize the makespan, because we do not believe it to be the main or the only scheduling metric to optimize. Hence, our observations have been conducted on metrics among which some come up from system environments and continuous job stream studies. We have observed our experiments on the following metrics:

- the **makespan**: it is the completion time of the last finished task, $\max_i C_i$. The makespan is an application metric, for it is its finishing date. So, even if it is the most used (basically with the MCT heuristic in Legion [GW97], NetSolve [CD96]), we do not think it is the appropriate metric to use when considering the client-agent-server model on the grid. Indeed, the agent can be requested by more than one user, so the agent does not necessarily deal with a single application, but must do its best for each of them.
- the **sumflow** [Bak74]: this is the amount of time that the completion of all tasks has taken on all the resources, $\sum_i (C_i - a_i)$. Executing tasks on servers has a cost proportional to the time it takes. We can therefore consider it as a system and economics metric, for it leads to estimate the profit realized by using a given heuristic when the cost of each resource is the same.

- the **maxstretch** [BCM98]: we know by this value by what maximum factor, $\max_i ((C_i - a_i)/d_i)$, a query has been slowed down relative to the time it takes on the same but unloaded server. A client can have an approximation of the minimum time his task will take on a server, but a task can require much more time than it would due to contention with previously allocated tasks and with hypothetical arriving ones. This value gives the worst case of slowdown for a task among all those submitted to the agent.
- the **maxflow** [BCM98]: this is the maximum time a task has spent in the system, $\max_i(C_i - a_i)$. In a loaded system, a task will generally cost more than expected. This is even truer if it is allocated on a fast server (which is generally more solicited). This value can inform about high contention or about the use of the slowest servers in a high heterogeneous system.
- the **meanflow** which is also in our context where tasks are executed as soon as the input data is received the mean response-time.
- the **percentage of tasks that finish sooner**: whereas this is not a metric, this value gives, in correlation to the previous metrics, a relevant idea of a quality of service given to each task when comparing two heuristics. For instance, comparing the heuristics H_1 with MCT (on the *same* set of tasks $\{t_1 \dots t_n\}$ and *same* environment), it is $\mid \{t_i | C_{t_i H_1} < C_{t_i MCT}\} \mid$ divided by n.

  The user point of view is not that the last allocated task finishes the soonest (optimizing the makespan) but that his own tasks (a subset of all client requests) finish as fast as possible. Therefore, if we can provide a heuristic where most of the tasks finish sooner than MCT's without delaying too much other task completion dates (that can be verified with the sum-flow and the response-time for example), we can claim that this heuristic, to the user point of view, outperforms MCT.

```
1  For each new task t
2      For each server j that can resolve the new submitted problem
3          Ask the HTM to compute the completion date of t, T_t, if t is executed on j
4      Map task t to server j_0 that minimizes T_t
5      Tell the HTM that task t is allocated to server j_0
```

Figure 2. *HMCT algorithm*

```
1  For each new task t
2      For each server j that can resolve the new submitted problem
3          Ask the HTM to compute P_j = sum_i delta_i
4      If all P_j are equal
5          map task to server j_0 that minimizes T_t
6      Else Map task t to server j_0 such as P_{j_0} = min_j P_j
7      Tell the HTM that task t is allocated to server j_0
```

Figure 3. *MP algorithm*

4. Proposed Heuristics

We have conducted several simulated experiments with the Simgrid API [Cas01]. Our investigations on several heuristics are reported in [CJ02] where independent tasks have been submitted to the environment. Among them, some heuristics gave good results on most of the metrics observed here. Indeed, in the simulated experiments, these did generally not only optimize the makespan but also one or more other metrics. We only describe in this section three of them that we have implemented and tested in real NetSolve environments: HMCT, MP and MSF.

When a new request arrives, the HTM simulates the execution of the task on each server. Our heuristics use the HTM information, hence consider the perturbation that tasks induce on each other and compute the 'best' server given an objective which is explained.

4.1. Historical Minimum Completion Time

HMCT is the MCT [MAS+99], Minimum Completion Time, algorithm relying on the HTM, in the time-share model. When a new task arrives, the HTM simulates the mapping of the task on each server. Therefore, the scheduler has an estimation of the finishing date of this task on each server. The agent then allocates the task to the server that minimizes its finishing date (see Fig. 2). Unlike MCT, which has been studied in the space-share model, HMCT do not assume a constant behavior of the environment during the execution of the task to predict its finishing date (see Section 2.1). HMCT uses HTM estimations which are far more precise.

The goal of HMCT is the same as MCT's: it expects to minimize the makespan of the application by minimizing the completion date of incoming tasks.

The main drawback of this heuristic is that it tends to overload the fastest servers, which has two effects: unnecessarily delay task completion dates and servers may collapse, mainly due to a lack of memory or to the incapability to handle the too high throughput of requests.

1 **For each** new task t
2 **For each** server j that can resolve the new submitted problem
3 Ask the HTM to compute $P_j = \sum_i \delta_i + T_t - a_t$
4 Map task t to server j_0 such as $P_{j_0} = \min_j P_j$
5 Tell the HTM that task t is allocated to server j_0

Figure 4. *MSF algorithm*

4.2. Minimum Perturbation

In MP, the new task is mapped to the server j that minimizes the sum of perturbations the new allocated task will generate on the previously mapped tasks (Fig. 3). In the case of equality, for instance at the beginning, the server that minimizes the completion date of the last incoming task is chosen (HMCT policy). MP aims to provide a better quality of service to each task by delaying as less as possible already allocated tasks.

Its main drawback is that the utilization of resources can be sub-optimal: a task can be allocated to a slow server unnecessarily, for example when some servers are not already loaded.

Nevertheless, when all the servers are loaded, fastest ones are still more solicited.

4.3. Minimum Sum Flow

Minimum Sum Flow is a willing attempt to mix the advantages of HMCT and MP (to keep the makespan objective of HMCT and give a better quality of service to each task) and to reduce the time cost on resources. The

Scenario	Application(s)		Independent Tasks		Experiment	
	nbclients	width x depth	nbtasks	μ (sec)	nbseeds x nbrun	total nbtasks
(a) 500 independent dgemm tasks	-	-	500	20 and 15	4 x 3	500
(b) 500 independent tasks	-	-	500	20 and 15	3 x 3 , 3 x 5	500
(c) 1D-mesh	10	1x50	-	-	4 x 6	500
(d) 1D-mesh	10	1x variable	-	-	4 x 6	500
(e) 1D-mesh + 250 independent tasks	5	1x50	250	20	4 x 6	500
(f) stencil (task 1)	1	10x50	-	-	1 x 6	500
(g) stencil (task 3)	1	10x50	-	-	1 x 6	500
(h) stencil + 174 independent tasks	1	10x25	174	28	2 x 3	424
(i) stencil + 86 independent tasks	1	10x25	86	40	4 x 6	336
(j) stencil + 86 independent tasks	1	5x25	86	25	4 x 6	211

Table 2. Scenarios, modalities and number of experiments

heuristic uses the HTM to compute the sum of the whole flow when assigning the last task to each server. Hence, the heuristic returns the identity of server j_0 that minimizes the system sum flow, e.g.

$$\min_j\left(\sum_{k\neq j,i=1}^{i=n}(T'_{i,k}-a_{i,k})+\sum_{i=1}^{i=n+1}(T_{i,j}-a_{i,j})\right)$$

But as the difference between two values is only due to perturbations and to the new simulated task duration, the heuristic only needs to compute $\sum_{i=1}^{t-1}\delta_i + T_t - a_t$ for each server j, that is to say the perturbation of the last task on the server plus the HTM estimated length of the new task (Fig. 4). This heuristic is the same then *MTI* (Minimize Total Interference) proposed by Weissman in [Wei96].

5. Experiments

We have conducted simulation experiments to test several heuristics on the submission of independent tasks to an agent. Results are related in [CJ02].

A perfect modelling of a realistic environment including monitors is hard: for example, load information given by censors and the frequency of the communications must be simplified (we work in a shared CPU context and scheduling decisions rely on the accuracy of the information given by the censors which, for example, return the number of tasks in place of the result of the `'uptime'` command). The objective of this work is to evaluate some of them in a real scale. Moreover, we also want to test them in experiments involving applications showing task dependences. Hence, we have implemented the HTM and the three heuristics described in the previous section, HMCT, MP and MSF, that were *a priori* able to give good results in a real NetSolve platform. We have performed several experiments with different kind of applications.

We have compared our heuristics against an implementation of MCT (section 4.1, [MAS+99]), the scheduling heuristic used in NetSolve. The implementation in NetSolve of this heuristic benefits of some load correction mechanisms: when the load of a server variates more than a given value, the server sends a load report to the agent, in the limit of one message per 60 seconds. Moreover, a mechanism adds a value to the chosen server last recorded load in the agent to take note of the affectation for further scheduling. Finally, the agent is informed of the finishing of a task and corrects the recorded load accordingly, waiting for a censor load report.

We firstly describe the application models, the different kind of tasks that compose a submitted application and the modalities of the experiments. Then, we present in the corresponding subsection several sets of experiments, which we will refer next to scenarios, given in Table 2 (this table will be fully detailed in the next section).

5.1. Application Models, Task Types and Experiments Modalities

The experiments presented later are performed on a NetSolve environment composed of one client, one agent and four servers. The resources, given in Table 3, are distributed in the research center. They are interconnected with the research center network. Then, if servers are dedicated to the environment, the network is not. The set of servers composing the environment is given in the corresponding section.

A scenario involves one kind of task, which can be of the two following: dgemm or wastecpu. A dgemm is a matrix multiplication of the BLAS library. It needs more or less memory depending on the sizes of the matrices that we generate randomly. Because of the heterogeneity of the NetSolve platform, we had troubles with NetSolve using MCT. Indeed, servers collapsed as it is explained further. Hence, we have designed a CPU intensive task which requires no memory that we have called *wastecpu*.

Given a kind of task, we use three different input data, conducting to three different durations. A task has a uniform probability to be of each duration. The need of each task has been benchmarked, and the values has been made available directly in the code of NetSolve. Therefore, the HTM for our scheduling heuristics and NetSolve MCT use these values (Tables 4 and 5).

Dgemm tasks are multiplication of matrices of size 1200, 1500 or 1800. Parameters given to the wastecpu tasks are 200, 400, 600. We give in the next subsections what kind of task is used, and we refer to the fastest task by *type 1* (matrix of size 1200 or parameter equal to 200), an to the slowest task by *type 3* (matrix of size 1800 or parameter 600).

The submission of an independent task set can be submissions by one client of all of the tasks or at least one request by several clients. Previous works use that class of application to evaluate their performances [BSB+99, MAS+99]. As we explain later, we cannot expect a high difference on the makespan performance with MCT on that kind of submission.

Results on independent tasks submission experiments led us to envisage the submission of applications with precedence relations. But, as far as we know, there is no real structural benchmark for a typical application model submitted in the client-agent-server model. Therefore, we have chosen to use linear applications, e.g. 1D mesh applications (fig 5), and stencil applications (fig 6) as applications implying precedence relations.

Concerning the 1D-mesh applications, we refer to the first task of the application by the *head*, to the last one by the *tail* of the application and the number of tasks is called its size. Each task, except the tail, has one unique daughter, and as soon as a task finishes (e.g. when the client has finished to receive the result from the server), the client requests the agent for the following task.

Stencil graph are composed of only one kind of task like in [BBR01]. Two other main information describe this graph: the width and the depth. Hence, there are *width* tasks composing the head of the graph and *width* tasks composing the tail. Except for these ones, a task have two or three fathers and two or three daughter. Next, we will refer to the task which is on the *ith* line and *jth* column by the task ij, the first task is noted (0,0).

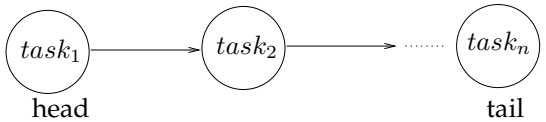

Figure 5. A 1D mesh application composed of n tasks

Table 2 summarizes all the scenarios that we have investigated. One can see that we have performed 10 different scenarios from (a) to (j). A scenario consists in the submission of applications and/or independent tasks.

type	machine	processor	speed	memory	swap	system
server	spinnaker	xeon	2 GHz	1 Go	2 Go	linux
	artimon	pentium IV	1.7 GHz	512 Mo	1024 Mo	linux
	pulney	xeon	1.4 GHz	256 Mo	533 Mo	linux
	cabestan	pentium III	500 MHz	192 Mo	400Mo	linux
	valette	pentium II	400 MHz	128 Mo	126 Mo	linux
	chamagne	pentium II	330 MHz	512 Mo	134 Mo	linux
	soyotte	sparc Ultra-1		64 Mo	188 Mo	SunOS
	fonck	sparc Ultra-1		64 Mo	188 Mo	SunOS
agent	xrousse	pentium II bipro	400 MHz	512 Mo	512 Mo	linux
client	zanzibar	pentium III	550 MHz	256 Mo	500 Mo	linux

Table 3. Resources of the testbed

size of the	memory need (Mo)		phase	time in seconds			
square matrix	input	output		pulney	artimon	cabestan	chamagne
1200	21.97	10.98	input sending time	3	3	4	4
			computing time	14	18	70	149
			output sending time	1	1	1	1
1500	34.33	17.16	input sending time	5	5	5	6
			computing time	25	33	136	292
			output sending time	1	1	2	2
1800	49.43	24.72	input sending time	7	8	8	8
			computing time	40	53	231	504
			output sending time	2	2	3	3

Table 4. Dgemm tasks' needs

parameter	phase	time in seconds					
		spinnaker	artimon	cabestan	valette	soyotte	fonck
200	input sending time	0.09	0.12	0.1	0.08	0.10	0.16
	computing time	16	17.1	74.86	97.81	128.09	127.56
	output sending time	0.05	0.03	0.03	0.03	0.06	0.05
400	input sending time	0.14	0.13	0.09	0.08	0.18	0.16
	computing time	30.6	33.2	148.48	182.52	255.56	254.09
	output sending time	0.06	0.03	0.03	0.03	0.06	0.05
600	input sending time	0.09	0.14	0.08	0.13	0.14	0.16
	computing time	45.6	49.4	222.26	273.28	382.5	380.66
	output sending time	0.05	0.03	0.03	0.03	0.06	0.05

Table 5. Wastecpu tasks' needs

The number of clients gives the number of applications involved in a scenario. The definition of the DAG of an application is given in the form width per depth. Information are given on independent tasks when some are submitted during the execution of applications. Their number and the rate at which they arrive (the inter-arrival time is drawn from a Poisson distribution). Each scenario is composed of $nbseeds$ different experiments that are executed $nbrun$ times from where no variation in the results is observed. Finally, the total number of tasks involved in a scenario is given.

The following modalities are true for each set of experiments:

- The platform is made of one client, one agent and the number of servers is held to 4. The name of the servers registered to the agent is given in the corresponding subsection. The reader can refer to Table 3

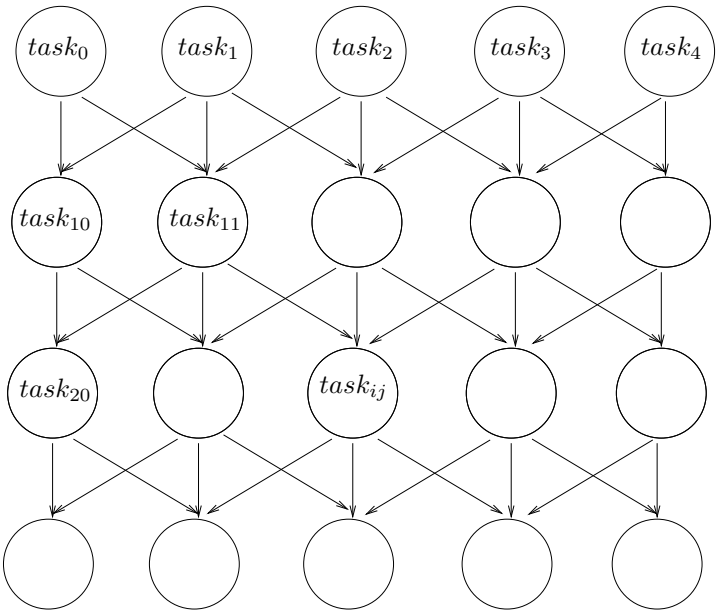

Figure 6. 5x4 stencil task graph

to have further information on the platform resources. We call *heterogeneity coefficient* of the platform, the maximum on all servers and on all tasks of the division of the maximum computing need by the minimum computing need for the same task, e.g. $\max_{task_i} \frac{\max_{servers} d_{i,s}}{\min_{servers} d_{i,s}}$;

- Only one kind of task (dgemm or wastecpu) is used to generate all the submitted applications in a scenario. Moreover, the same experiment has been carried out several times (equal to $nbrun$ given in Table 2). This is referred to as a *run*. Results are means on these runs ;
- There is 3 different possible sizes when a task of a given type is drawn. Then, one can generate 3^n different applications composed of n tasks ;
- We note that in each experiment of each scenario, a scheduling decision cost is negligible compared to the duration of the shortest task (less than 0.1 second) for all the proposed heuristics.

5.2. Scenarios (a) and (b): Submission of 500 Independent Tasks

We present two kind of submissions with scenario (a) and (b): the first scenario is composed of dgemm tasks and the second is made of wastecpu tasks. As we consider in this paper three possible inputs, one can generate 3^{500} different sets of independent tasks for one experiment in each scenario. Given a generated set of tasks, the difference between two arrival dates is drawn from a Poisson distribution with a mean of $\mu = 20$ seconds and $\mu = 15$ seconds.

In the following, we describe more precisely the two scenarios then we explain the results.

5.2.1 Scenario (a): Dgemm Independent Tasks Submission

In the first set of experiments, the tasks are multiplications of square matrix (dgemm) of size 1200, 1500 and 1800 leading to different time and memory cost (Table 4). The platform, described next, has an heterogeneous coefficient equal to $504/40 = 12.6$. For all the experiments, the testbed is composed of:

- client: zanzibar ;
- agent: xrousse ;

	NetSolve's MCT	HMCT	MP	MSF
number of completed tasks	500	500	500	500
makespan	9906	9908	10162	9905
sumflow	25922	19934	26383	19702
maxflow	230	103	517	97
maxstretch	12.8	5.8	3.7	5.3
percentage of tasks that finish sooner than with NetSolve's MCT	-	65%	66%	65%

Table 6. Scenario (a): results in seconds for $\mu = 20$ sec for dgemm Tasks

	NetSolve's MCT	HMCT	MP	MSF
number of completed tasks	495	358	500	500
makespan	7880	5600	7648	7626
sumflow	89254	25092	34677	31375
maxflow	1780	500	720	250
maxstretch	99	27.8	6.3	11.3
percentage of tasks that finish sooner than with NetSolve's MCT	-	<85%>	84%	87%

Table 7. Scenario (a): results in seconds for $\mu = 15$ sec for dgemm Tasks

- servers: chamagne ; pulney ; cabestan ; artimon.

Results on the makespan, the sumflow for $\mu = 20$ seconds are given in Table 6 summarizes mean results for $\mu = 20$ seconds on the number of completed tasks, the makespan, the sumflow, the maxflow, the maxstretch and the percentage of tasks that finish sooner than if scheduled with MCT.

In Table 7, where $\mu = 15$ and built the same way than the previous one, values for MCT and HMCT results are those obtained from the run when the number of completed tasks was the maximum. Indeed, for $\mu = 15$, MCT and HMCT are not able to handle the throughput of tasks. HMCT and MCT overload the fastest servers that cannot accept any more jobs because they run out of memory. However, the NetSolve MCT has fault tolerance mechanisms that permit to schedule almost all tasks on some runs. For $\mu = 20$, this phenomenon does not occur because the arrival rate lets faster servers complete more tasks before a new request.

One should note that for $\mu = 15$ seconds, the NetSolve MCT gives very high values, and the highest for all the observed metrics, showing lesser performances. There is a huge time and space contention on the fastest servers. This is confirmed, for MCT and for HMCT, by the load average sent to the agent (more than 12 on pulney). Consequently, some servers collapsed during the experiment.

Even when there is low contention, e.g. when $\mu = 20$ seconds, one can see from the results that using an heuristic that uses HTM information leads to better performances than MCT benefiting from load correction mechanisms. From these results, MSF is the best heuristic: it achieves the best performances regardless the metric and the rate of incoming submissions.

5.2.2 Scenario (b): Wastecpu Independent Tasks Submission

We use wastecpu tasks to prevent memory problems that we do not yet handle. The goal is to replace the multiplication tasks, so its computation costs, dependent on the parameters, are similar to the multiplication tasks. A wastecpu task can have the parameter 200, 400 or 600 which determines the time it costs (Table 5).

Two platform have been used. We give next the experimentations and the results obtained for each of them. For the both of them, we can remark with relief that two runs of the same experiment give slightly the same results. This explains the small number of experiments undertaken. Moreover, for this scenario, all tasks of each set have been submitted, accepted and computed by all of the five heuristics we have tested.

Platform 1 The heterogenous coefficient (the maximum computing cost divided by the minimum for the same task) of the platform described next is $97/16 = 6$. The experimental testbed for this set of experiments is made up of:

- client: zanzibar ;
- agent: xrousse ;
- servers: valette ; spinnaker ; cabestan ; artimon.

We generated three different sets of tasks, submitted at two different arrival rates. Results for $\mu = 20$ seconds, given in Table 9, are obtained from 2 executions of the same metatask scheduled by each of the four tested heuristics. At this rate, the experiment finishes after about $10,000$ seconds. In Table 8, for $\mu = 15$ seconds, values are the mean of 4 executions for the NetSolve MCT and 3 for the three others. At this rate, the experiment needs about $7,700$ seconds to complete. For a set of independent tasks scheduled according to a given heuristic, the percentage of tasks that finish sooner is the mean of the values obtained from the comparison between each run for this heuristic and each run for NetSolve (hence obtained from a comparison in '*cross product*'). Finally, we give in the column 'Avg' the mean on the observed metric of the values obtained for each run and each set.

HMCT and MSF outperform MCT regardless the rate and the observed metric. If they give slightly the same results for $\mu = 20$, MSF even outperforms HMCT when $\mu = 15$ seconds. On the opposite, MP shows performance gains only for $\mu = 15$ seconds. Our heuristics are specifically designed for environments with contention: gains increase with it.

	NetSolve's MCT				HMCT				MP				MSF			
	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**
makespan	7690	7615	7644	**7650**	7655	7565	7626	**7615**	7672	7545	7765	**7661**	7672	7544	7626	**7614**
sumflow	63364	49529	50014	**54302**	39973	36675	34821	**37156**	33913	30860	30158	**31644**	34347	30279	29744	**31457**
maxflow	344	283	290	**306**	234	231	228	**231**	340	314	314	**323**	234	182	162	**193**
maxstretch	7.5	6.5	6.7	**6.9**	4.9	5	4.6	**4.8**	3.8	3.2	2.9	**3.3**	5	3.4	3.2	**3.9**
number of tasks that finish sooner than with NetSolve's MCT	-	-	-	–	78.6%	73.6%	77.6%	**76.6**%	83.2%	80.6%	82%	**82**%	84.6%	80.4%	82.4%	**82.4**%

Table 8. Scenario (b), platform 1: results in seconds for $\mu = 15$ sec for wastecpu Tasks

	NetSolve's MCT				HMCT				MP				MSF			
	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**
makespan	9913	10044	10210	**10056**	9901	10041	10210	**10051**	10009	10047	10265	**10107**	9903	10041	10209	**10051**
sumflow	25768	22036	20727	**22844**	20151	18151	17364	**18555**	26729	24384	24239	**28451**	20306	18138	17317	**18587**
maxflow	193	168	124	**162**	123	109	82	**105**	286	275	273	**278**	116	135	85	**112**
maxstretch	4.1	4.1	2.8	**3.7**	3.1	2.2	2.1	**2.4**	1.8	1.8	2	**1.9**	2.8	2.8	2.2	**2.6**
percentage of tasks that finish sooner than with NetSolve's MCT	-	-	-	–	68.8%	62.8%	64.8%	**65.4**%	67.8%	63.4%	64.2%	**65.2**%	66.2%	61.8%	64%	**64**%

Table 9. Scenario (b), platform 1: results in seconds for $\mu = 20$ sec for wastecpu tasks

Platform 2 The heterogeneous coefficient of the second platform is slightly superior to the previous and equal to 8.9. The following resources composed the environment:

- client: zanzibar ;
- agent: xrousse ;
- servers: spinnaker, artimon, soyotte, fonck.

Three different seeds have been used to instantiate Scenario (b), and the resulting experiments have been submitted at three different rates: 20, 17 and 15 seconds. For $\mu = 17$ and $\mu = 20$ seconds, each experiment has been submitted 3 times conducting to 9 submissions per rate and per heuristic for this scenario. For $\mu = 15$ seconds, each experiment has been submitted 6 times then 15 submissions have been performed on the platform for this rate and for each heuristic. Tables presenting the results for $\mu = 20$ are detailed next. Tables for $\mu = 17$ and $\mu = 15$ are built the same way.

Results for the inter-arrival $\mu = 20$ seconds are given in Tables 10, 11, 16. We describe in Table 10 the utilization of each server by each heuristic during each experiment: given an experiment, each percentage of allocated tasks on the 500 of the experiment (the corresponding part of each task type is precised in parenthesis) per server is given. The sumflow per server as well as the total sumflow that the experiment costs is also given.

Table 11 gives the mean flow recorded during the submission of the experiment scheduled by MCT and the average gain for each task type over MCT if the same experiment is scheduled by a given heuristic.

Table 16 summarizes many information: for each heuristic and each seed, mean results on the makespan, the sumflow, the maxflow, the maxstretch and the number of tasks finishing sooner than if scheduled by MCT are given.

Like for the previous platform, for each seed and each heuristic (naturally except MCT) the percentage of tasks that finish sooner is the average percentage obtained from the comparison of terminaison dates between each run for this heuristic and each run for NetSolve (hence from a comparison in '*cross product*'). A task is considered 'finishing sooner' if the terminaison dates differ from at least 2 seconds between MCT and the other heuristic. Thus, we give in parenthesis the percentage of tasks that finish sooner with MCT than with the given heuristic: because there exists tasks that finish in a range of 2 seconds between a run with MCT and with another heuristic, the sum of the percentage of tasks that finish sooner with our heuristic and the percentage of tasks that finish sooner with MCT differs from 100. Finally the column 'Avg' contains the mean on the observed metric of the values for each run and each seed.

The same experiments have been conducted with $\mu = 17$ and $\mu = 15$ seconds and we present the results respectively in Tables 12, 13, 17 and in Tables 14, 15, 18.

With Tables 10, 12 and 14, one can see the evolution of the processor utilization in function of the heuristic. Regardless the heuristic, the percentage of tasks scheduled on spinnaker decreases slightly: all types of tasks are concerned in the same manner. This benefits to the slower servers: only to artimon for HMCT, but MP and MSF give also more jobs to fonck and soyotte.

If HMCT and MSF have the same behavior and outperform both MP and MCT for $\mu = 20$ and $\mu = 17$, MP achieves to reduce the total sumflow progression and outperfom all the others for $\mu 15$ seconds.

Table 11 confirms that for slow rate, MP achieve sub-optimal scheduling. The average gain over MCT is negative: each task scheduled by MCT is 28% shorter than with MP. On the opposite, at this rate, HMCT and MSF show nearly the same positive results: their scheduling leads to gain 20% on each task flow. Due to perturbations, when the rate increases to $\mu = 17$ seconds, the average flow grows to 160% bigger with MCT. All of our heuristics outperfom MCT, HMCT and MSF maximising the gains for each task, allowing them to be 26% shorter. When the rate is high ($\mu = 15$), MP achieves the best gains with an average flow 42% shorter than for MCT.

experiment 1								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	56.9 (18.7 16.5 21.7)	12463	60.2 (19.6 18.0 22.6)	10344	52.6 (17.4 15.2 20.0)	8103	58.6 (19.4 16.8 22.4)	9959
artimon	43.1 (13.9 13.1 16.1)	9447	39.8 (13.0 11.6 15.2)	7381	35.2 (10.8 10.4 14.0)	6307	41.4 (13.2 12.8 15.4)	7712
soyotte	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	5.4 (1.6 1.8 2.0)	7185	0.0 (0.0 0.0 0.0)	0
fonck	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	6.8 (2.8 2.2 1.8)	8029	0.0 (0.0 0.0 0.0)	0
total sumflow		21910		17725		29624		17671
experiment 2								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	57.3 (17.9 19.4 20.0)	13515	58.8 (17.6 21.2 20.0)	10196	52.2 (15.8 19.0 17.4)	7949	58.6 (18.8 20.8 19.0)	10002
artimon	42.7 (12.7 15.8 14.2)	10662	41.2 (13.0 14.0 14.2)	7981	37.2 (12.0 13.2 12.0)	6319	41.4 (11.8 14.4 15.2)	8180
soyotte	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	4.8 (1.0 1.6 2.2)	6916	0.0 (0.0 0.0 0.0)	0
fonck	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	5.8 (1.8 1.4 2.6)	7885	0.0 (0.0 0.0 0.0)	0
total sumflow		24177		18177		29069		18182
experiment 3								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	57.8 (21.7 19.9 16.2)	11307	61.3 (22.1 19.9 19.3)	9908	54.4 (19.8 17.4 17.2)	7907	59.6 (21.2 19.2 19.2)	9617
artimon	42.2 (14.3 14.1 13.8)	8922	38.7 (13.9 14.1 10.7)	6745	36.0 (12.6 13.8 9.6)	5809	40.4 (14.8 14.8 10.8)	6978
soyotte	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	4.0 (0.8 1.6 1.6)	5640	0.0 (0.0 0.0 0.0)	0
fonck	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	5.6 (2.8 1.2 1.6)	6377	0.0 (0.0 0.0 0.0)	0
total sumflow		20229		16653		25733		16595
MEAN								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	57.3 (19.4 18.6 19.3)	12428	60.1 (19.8 19.7 20.6)	10149	53.1 (17.7 17.2 18.2)	7986	58.9 (19.8 18.9 20.2)	9859
artimon	42.7 (13.6 14.3 14.7)	9677	39.9 (13.3 13.2 13.4)	7369	36.1 (11.8 12.5 11.9)	6145	41.1 (13.3 14.0 13.8)	7623
soyotte	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	4.7 (1.1 1.7 1.9)	6580	0.0 (0.0 0.0 0.0)	0
fonck	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	6.1 (2.5 1.6 2.0)	7430	0.0 (0.0 0.0 0.0)	0
total sumflow		22105		17518		28142		17483

Table 10. Scenario (b), platform 2: processors utilization for $\mu = 20$ seconds

		mean flow	gain in **percentage**		
		MCT (sec)	HMCT	MP	MSF
	type 1	22.1	14.5	-44.9	14.9
experiment 1	type 2	42.6	20.8	-45.2	21.8
	type 3	63.5	19.6	-27.1	19.4
	type 1	23.2	21.5	-15.6	22.1
experiment 2	type 2	47.5	25.0	-6.6	24.9
	type 3	71.7	25.6	-30.9	25.5
	type 1	20.3	12.1	-35.8	11.8
experiment 3	type 2	41.1	18.6	-21.2	19.1
	type 3	64.0	19.2	-28.3	19.5
MEAN	-	44.0	19.7	-28.4	19.9

Table 11. Scenario (b), platform 2: average percentage gain for $\mu = 20$ sec on each task given by type

server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
experiment 1								
spinnaker	56.0 (19.0 17.0 20.0)	20527	55.0 (17.4 17.0 20.6)	14147	49.9 (16.9 14.5 18.5)	8719	55.4 (18.6 16.4 20.4)	13489
artimon	44.0 (13.6 12.6 17.8)	16235	45.0 (15.2 12.6 17.2)	12179	38.1 (11.2 11.4 15.5)	7752	44.2 (13.6 13.2 17.4)	11992
soyotte	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	6.3 (2.8 1.9 1.5)	7280	0.0 (0.0 0.0 0.0)	0
fonck	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	5.8 (1.7 1.8 2.3)	7887	0.4 (0.4 0.0 0.0)	257
total sumflow		36762		26326		31638		25738
experiment 2								
spinnaker	54.8 (16.9 18.2 19.7)	20242	55.4 (15.6 22.2 17.6)	15647	51.0 (16.6 18.9 15.5)	8579	54.8 (15.8 21.0 18.0)	14520
artimon	45.2 (13.7 17.0 14.5)	17863	44.6 (15.0 13.0 16.6)	13588	37.5 (10.9 12.1 14.5)	7840	44.4 (14.0 14.2 16.2)	13884
soyotte	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	6.2 (2.0 2.5 1.7)	7839	0.2 (0.2 0.0 0.0)	130
fonck	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	5.3 (1.1 1.7 2.5)	7781	0.6 (0.6 0.0 0.0)	386
total sumflow		38105		29235		32039		28920
experiment 3								
spinnaker	57.2 (20.9 19.8 16.5)	17342	54.8 (18.2 18.2 18.4)	12325	50.8 (18.8 17.2 14.8)	8134	53.2 (16.6 18.4 18.2)	11915
artimon	42.8 (15.1 14.2 13.5)	13929	45.2 (17.8 15.8 11.6)	10208	37.6 (12.8 12.6 12.2)	6917	46.6 (19.2 15.6 11.8)	10313
soyotte	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	5.4 (2.0 1.6 1.8)	6888	0.0 (0.0 0.0 0.0)	0
fonck	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	6.2 (2.4 2.6 1.2)	7248	0.2 (0.2 0.0 0.0)	130
total sumflow		31271		22533		29187		22358
MEAN								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	56.0 (18.9 18.3 18.8)	19370	55.1 (17.1 19.1 18.9)	14040	50.6 (17.4 16.8 16.3)	8477	54.5 (17.0 18.6 18.9)	13308
artimon	44.0 (14.2 14.6 15.2)	16009	44.9 (16.0 13.8 15.1)	11992	37.7 (11.6 12.0 14.1)	7503	45.1 (15.6 14.3 15.1)	12063
soyotte	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	6.0 (2.3 2.0 1.7)	7336	0.1 (0.1 0.0 0.0)	43
fonck	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	5.8 (1.8 2.0 2.0)	7639	0.4 (0.4 0.0 0.0)	258
total sumflow		35379		26031		30955		25672

Table 12. Scenario (b): processors utilization for $\mu = 17$ seconds

		mean flow	gain in percentage		
		MCT (sec)	HMCT	MP	MSF
experiment 1	type 1	35.7	21.1	0.3	21.5
	type 2	71.6	27.7	11.4	29.0
	type 3	107.6	30.9	19.2	32.9
experiment 2	type 1	36.3	22.4	15.5	18.5
	type 2	73.5	22.3	13.9	24.6
	type 3	114.7	24.2	17.4	25.4
experiment 3	type 1	31.9	21.6	-1.9	22.3
	type 2	59.6	27.2	-3.1	27.4
	type 3	102.6	30.8	16.3	31.6
MEAN	-	70.4	25.4	9.9	25.9

Table 13. Scenario (b), platform 2: average percentage gain for $mu = 17$ sec on each task given by type

server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
experiment 1								
spinnaker	53.2 (17.3 15.7 20.2)	42566	50.2 (13.7 15.9 20.6)	26124	48.8 (16.9 14.2 17.7)	11918	49.4 (13.0 16.0 20.4)	19824
artimon	45.5 (14.7 13.6 17.2)	38915	44.8 (13.9 13.7 17.2)	28713	40.0 (12.3 11.8 15.8)	11272	44.0 (13.8 12.8 17.4)	19596
soyotte	0.6 (0.3 0.1 0.2)	693	2.2 (2.2 0.0 0.0)	1431	5.2 (1.0 2.2 2.0)	7749	3.2 (3.0 0.2 0.0)	2238
fonck	0.7 (0.2 0.2 0.3)	945	2.8 (2.8 0.0 0.0)	1891	6.0 (2.3 1.3 2.3)	8084	3.4 (2.8 0.6 0.0)	2578
total sumflow		83119		58159		39023		44236
experiment 2								
spinnaker	53.3 (16.4 18.6 18.3)	38279	-	-	49.3 (16.5 17.3 15.5)	13346	50.8 (14.4 18.0 18.4)	19274
artimon	44.8 (13.9 15.8 15.1)	33412	-	-	40.2 (12.2 13.4 14.6)	12309	44.2 (13.0 15.4 15.8)	21121
soyotte	0.9 (0.1 0.5 0.3)	2468	-	-	5.6 (1.2 2.7 1.7)	8409	2.0 (1.0 1.0 0.0)	2073
fonck	1.0 (0.2 0.3 0.4)	2695	-	-	4.8 (0.7 1.8 2.4)	7996	3.0 (2.2 0.8 0.0)	2662
total sumflow		76854		-		42060		45130
experiment 3								
spinnaker	55.0 (20.9 17.7 16.4)	25061	53.8 (19.1 18.8 15.9)	18870	47.7 (15.9 17.1 14.7)	9865	53.0 (18.2 19.3 15.5)	17279
artimon	45.0 (15.1 16.3 13.6)	21586	46.2 (16.9 15.2 14.1)	18181	41.2 (16.4 13.8 11.0)	9136	45.4 (16.5 14.5 14.5)	16303
soyotte	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	6.0 (2.6 1.6 1.8)	7562	0.7 (0.7 0.0 0.0)	465
fonck	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	5.1 (1.1 1.5 2.5)	7672	0.8 (0.6 0.2 0.0)	664
total sumflow		46647		34235		34711		
MEAN								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	53.8 (18.2 17.3 18.3)	35302	<52.0 (16.4 17.3 18.3)>	<22497>	48.6 (16.4 16.2 16.0)	11710	51.1 (15.2 17.8 18.1)	18792
artimon	45.1 (14.6 15.2 15.3)	31304	<45.5 (15.4 14.5 15.6)>	<23447>	40.5 (13.7 13.0 13.8)	10906	44.5 (14.4 14.2 15.9)	19007
soyotte	0.5 (0.1 0.2 0.2)	1054	<1.1 (1.1 0.0 0.0)>	<716>	5.6 (1.6 2.2 1.8)	7907	2.0 (1.6 0.4 0.0)	1592
fonck	0.6 (0.2 0.2 0.2)	1213	<1.4 (1.4 0.0 0.0)>	<946>	5.3 (1.4 1.5 2.4)	7917	2.4 (1.9 0.5 0.0)	1968
total sumflow		68873		<47605>		38439		41359

Table 14. Scenario (b): processors utilization for $\mu = 15$ seconds

		mean flow	gain in percentage		
		MCT (sec)	HMCT	MP	MSF
experiment 1	type 1	83.6	18.7	52.4	31.7
	type 2	162.8	31.6	51.1	47.2
	type 3	234.5	31.8	53.2	50.2
experiment 2	type 1	67.7	-	48.0	28.2
	type 2	151.6	-	42.2	40.0
	type 3	230.7	-	46.3	45.4
experiment 3	type 1	51.8	19.7	31.7	23.3
	type 2	95.3	23.7	35.1	30.3
	type 3	144.0	20.4	19.8	25.7
MEAN	-	135.8	<24.3>	42.2	35.8

Table 15. Scenario (b): average percentage gain for $\mu = 15$ sec on each task given by type

	NetSolve's MCT				HMCT				MP				MSF			
	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**
makespan	10134	9934	10033	**10034**	10118	9918	10022	**10019**	10456	10231	10157	**10281**	10118	9917	10021	**10019**
sumflow	21910	24176	20229	**22105**	17726	18177	16653	**17519**	29625	29070	25734	**28143**	17671	18182	16594	**17482**
maxflow	136.4	163.5	142.1	**147.3**	74.2	117.1	91.3	**94.2**	398.5	390.8	390.8	**393.4**	82.3	114.4	91.2	**96.0**
maxstretch	3.6	4.2	3.7	**3.8**	2.5	3.0	2.6	**2.7**	9.3	9.1	9.3	**9.2**	2.5	2.9	2.6	**2.7**
percentage of tasks that finish sooner than with NetSolve's MCT	-	-	-	–	55 (20)	59 (17)	50 (16)	**55(18)**	52 (20)	59 (18)	49 (18)	**53(19)**	56 (19)	60 (17)	50 (16)	**55(17)**

Table 16. Scenario (b): results in seconds for $\mu = 20$ sec on wastecpu tasks

	NetSolve's MCT				HMCT				MP				MSF			
	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**
makespan	8525	8513	8557	**8532**	8513	8505	8517	**8512**	8831	8822	8825	**8826**	8500	8505	8517	**8507**
sumflow	36762	38105	31272	**35380**	26327	29235	22534	**26032**	31638	32039	29187	**30955**	25739	28920	22358	**25672**
maxflow	257.6	256.0	271.3	**261.7**	182.8	185.1	193.7	**187.2**	405.5	411.0	417.5	**411.3**	170.0	190.8	184.0	**181.6**
maxstretch	6.6	7.0	7.3	**7.0**	4.9	5.4	5.3	**5.2**	10.0	10.1	11.0	**10.4**	8.8	8.8	8.8	**8.8**
percentage of tasks that finish sooner than with NetSolve's MCT	-	-	-	–	71 (19)	70 (20)	66 (19)	**69(19)**	75 (18)	74 (17)	67 (19)	**72(18)**	71 (18)	69 (20)	67 (19)	**69(19)**

Table 17. Scenario (b): results in seconds for $\mu = 17$ sec on wastecpu tasks

	NetSolve's MCT				HMCT				MP				MSF			
	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**	$seed_1$	$seed_2$	$seed_3$	**Avg**
makespan	7697	7677	7577	**7650**	7645	-	7551	**7598**	7910	7899	7844	**7885**	7646	7650	7546	**7614**
sumflow	83120	76854	46647	**68874**	58159	-	37051	**47605**	39024	42060	34236	**38440**	44235	45130	34712	**41359**
maxflow	420.1	883.4	323.0	**542.2**	313.1	-	288.6	**300.8**	441.2	521.8	430.1	**464.4**	264.5	348.0	264.1	**292.2**
maxstretch	10.3	23.8	8.5	**14.2**	10.6	-	7.2	**8.9**	11.8	14.9	12.4	**13.0**	10.2	12.8	9.6	**10.8**
percentage of tasks that finish sooner than with NetSolve's MCT	-	-	-	–	84 (14)	-	76 (20)	**80(17)**	87 (12)	84 (14)	82 (15)	**84(14)**	88 (11)	84 (14)	76 (20)	**83(15)**

Table 18. Scenario (b): results in seconds for $\mu = 15$ sec on wastecpu tasks

5.2.3 Results

We have considered in this subsection the scheduling of a set of independent tasks whose inter-submissions follow a Poisson distribution of parameter μ equal to 15, 17 or 20 seconds. Therefore, the makespan is strongly dependent on the latest task arrival. We cannot expect at the very outset a big difference between two heuristics on that metric especially at low rate [MAS+99], even in a CPU shared environment. That is verified by our tests. Nonetheless, heuristics do not have the same performances.

The overall results converge even if gains are a bit better on the experiments performed on Platform 2: at the same rate, there is more contention as the heterogeneity increases. Thus our heuristics that are designed to take into account the contention behave even better.

One can note that MCT and HMCT tend to not use the slowest servers fonck and soyotte. Indeed, a task has to finish sooner on soyotte than on spinnaker to be scheduled there: this implies sufficient perturbations to do so, i.e. that during the execution of the task on spinnaker a number of tasks superior to the heterogeneity coefficient be running concurrently for HMCT as well as an sufficient load on artimon as well. This clearly limits the throughput of tasks and even make HMCT unable to handle the second experiment on the platform 2 when $\mu = 15$ seconds.

To see how useful the HTM is, we compare results on the same heuristic: MCT and HMCT (in fact, these are not exactly the same due to NetSolve load correction mechanisms). We see in Table 9 that HMCT needs one missing hour (4289 seconds) of computations for a set of independent tasks whose time cost is of less than three hours ($\mu = 20$) for the same makespan. Its performances are greater as the rate increases: a gain of 4.8 hours of computations for a duration of 2.1 hours, and there too, a better quality of service (Table 8).

Moreover, a better quality of service is offered regardless the rate: HMCT shows a gain in average response time in Tables 11, 13 and 15 but cases exist where it cannot handle the throughput of submissions. Results are always better for HMCT, and gains increase with the rate (see Tables 16, 17 and 18).

In consequence, the use of the HTM definitely leads to better results for Scenario (a) and (b), where the set of independent tasks can be perceived as one client with many tasks or many clients with at least one tasks.

MP has a better load balance property than MCT and HMCT (Table 9 and 8). Hence, when μ is large (low arrival rate), it loads slower servers because they are idle. Whereas, when μ is low, no servers are idle, then MP, like HMCT and MSF, tends also to load the fastest ones. MP presents the highest maxflow. It seems logical considering that:

- for $\mu = 20$, as tasks on faster servers are not necessarily finished, slower servers are used. The MP maxflow comes from the maximum cost of a task on the slowest server.
- for $\mu = 15$, there is contention even on the slowest servers. A task that had already a higher duration than if allocated to a faster server requires even more time.

Therefore at low rate, MP is sub-optimal, but is rather good at higher rates: less sumflow (even compared to MSF) and a high number of tasks that finish sooner than MCT.

MSF tries to optimize the sumflow, hence finds a good balance between minimizing the perturbation and minimizing the new task duration. Therefore, it gives good performances on the makespan, the sumflow, even on the maxflow and the percentage of tasks that finish sooner than with MCT is always very high (nearly the same than MP's for $\mu = 15$!). While MSF is not explicitly designed to optimize the makespan as is MCT, it appears that it always outperforms MCT, as well as HMCT and MP on most of the metrics. Considering that an agent cannot guess the rate of the requests it will have to process, MSF is the best because it gives the same performances than HMCT at low rates and better performances than others at higher rates.

5.3. Scenario (c): Submission of 10 1D-mesh Applications, Each Composed of 50 Wastecpu Tasks

An experiment consists in the submission of 10 applications composed of 50 wastecpu tasks each. An application is a 1D-mesh application (section 5.1), hence, when a client has received the result of its task, he immediately

sends a new request to the agent until the last task: the tail of the application.

One can generate for each client 3^{50} applications. Tasks needs are given in Table 5. We assume that the difference between two application head arrival dates (e.g. two client first submissions) follows a Poisson distribution with a mean of $\mu = 15$ seconds.

Four experiments have been generated, each with a different seed. Then, two experiments differ from each other in the arrival date of each client head as well as in the composition of applications (see Table 19).

The same experiment has been executed 6 times. As we will explain, even on exactly the same experiment, an heuristic can have a non negligible standard deviation on its results.

The heterogeneity coefficient of the platform, equal to $273.28/45.6 = 8.9$, is made of:

- client: zanzibar ;
- agent: xrousse ;
- servers: spinnaker, artimon, soyotte, fonck.

client	experiment 1			experiment 2			experiment 3			experiment 4		
	type 1	type 2	type 3	type 1	type 2	type 3	type 1	type 2	type 3	type 1	type 2	type 3
client 1	20	11	19	20	17	13	16	16	18	22	12	16
client 2	17	13	20	15	21	14	22	16	12	12	19	19
client 3	13	17	20	14	16	20	20	19	11	14	17	19
client 4	14	15	21	11	22	17	20	12	18	18	14	18
client 5	18	13	19	10	14	26	17	18	15	22	12	16
client 6	18	16	16	11	22	17	19	18	13	22	14	14
client 7	11	19	20	20	16	14	17	17	16	16	17	17
client 8	21	14	15	19	13	18	15	19	16	16	18	16
client 9	16	12	22	14	19	17	18	17	15	21	12	17
client 10	22	13	15	18	11	21	16	10	24	23	14	13
total	170	143	187	152	171	177	180	162	158	186	149	165

Table 19. Scenario (c): applications composition

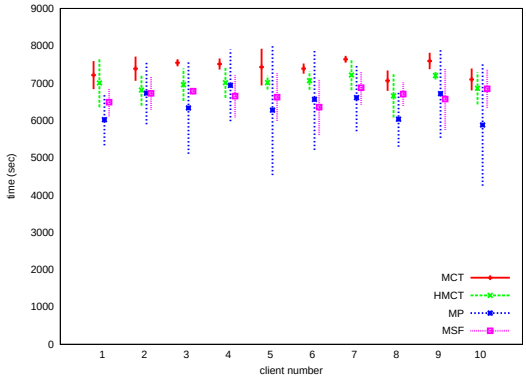

Figure 7. Scenario (c): Results on the makespan for the first experiment

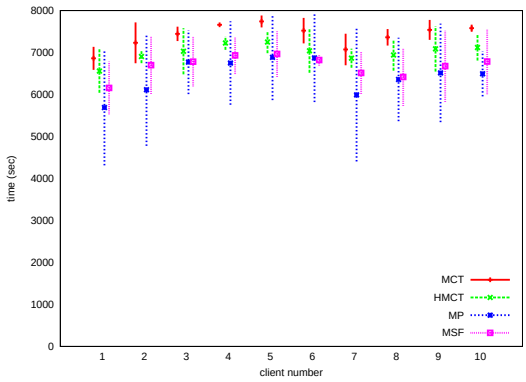

Figure 8. Scenario (c): Results on the makespan for the second experiment

We note that, at any time, all clients can have a request being computed in the distributed system. So, there is at most 10 tasks in the environment at a given moment.

Moreover, we must also note that, on the contrary of the previous section (submission of a set of independent tasks), scheduling decisions are not necessarily the same between two runs. With that kind of application, results can consequently differ between two runs. Indeed, the arrival date of a task can differ even slightly between two runs: a task can finish sooner or later than in another run. As precedence links exist, daughters might not be scheduled to same servers. This scenario leads immediately to a different run, especially if the scheduling heuristic has a tendency to use slower servers: all the next termination dates change due to scheduling decisions taken consequently to the system state, which differs. As all the tasks arrival dates of an application might differ, and due to the heterogeneity of the platform, the makespan for example can vary.

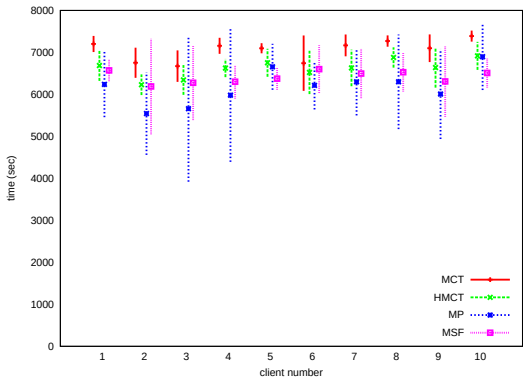

Figure 9. Scenario (c): results on the makespan for the third experiment

5.3.1 Results

The results of the 4 experiments are given in Figures 7, 8, 9, 10 and in Tables 20 and 21.

One can see in each graph the mean and the standard deviation of the makespan obtained on the 6 runs for each of the 10 submitted applications. As applications are 1D-mesh, we can consequently compare sumflows on these graphics if neglecting the head arrival date (due to the low value of head arrival dates, graphs are nearly identical). Indeed, for this kind of application, the makespan is the head arrival date added to the sumflow.

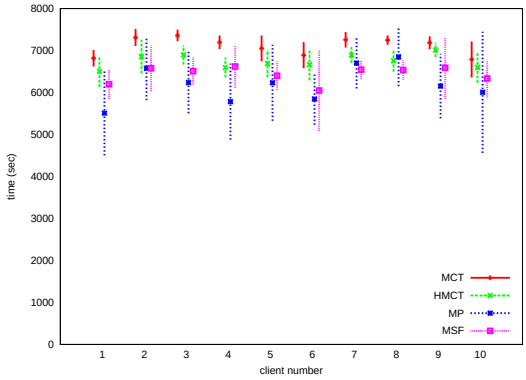

Figure 10. Scenario (c): results on the makespan for the fourth experiment

server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
experiment 1								
spinnaker	53.4 (17.7 15.6 20.1)	37506	47.1 (12.0 14.7 20.5)	28130	49.2 (17.7 13.7 17.8)	17206	46.0 (13.1 13.3 19.6)	21433
artimon	46.6 (16.3 13.0 17.3)	35442	42.3 (12.6 12.8 16.9)	32471	41.8 (14.9 12.5 14.3)	22269	39.4 (11.2 10.9 17.3)	27928
soyotte	0.0 (0.0 0.0 0.0)	0	5.0 (4.4 0.6 0.0)	3932	4.5 (0.7 1.2 2.6)	11837	7.0 (4.6 2.2 0.2)	8042
fonck	0.0 (0.0 0.0 0.0)	0	5.6 (5.0 0.6 0.0)	4344	4.5 (0.7 1.2 2.6)	11873	7.5 (5.0 2.2 0.3)	8308
total sumflow		72948		68877		63185		65711
experiment 2								
spinnaker	54.0 (16.8 18.2 19.0)	38121	47.9 (11.3 17.6 19.1)	27366	49.2 (15.9 16.2 17.1)	17367	45.9 (11.2 15.8 18.9)	21761
artimon	46.0 (13.6 16.0 16.4)	35012	42.2 (10.8 15.1 16.3)	33742	41.6 (13.6 14.2 13.8)	22521	40.2 (10.6 13.6 16.0)	27710
soyotte	0.0 (0.0 0.0 0.0)	0	4.4 (3.5 0.9 0.0)	3683	4.5 (0.4 1.8 2.3)	11758	6.5 (3.9 2.2 0.3)	7836
fonck	0.0 (0.0 0.0 0.0)	0	5.4 (4.8 0.6 0.0)	4355	4.6 (0.5 2.0 2.2)	11914	7.4 (4.7 2.5 0.2)	8564
total sumflow		73133		69146		63560		65871
experiment 3								
spinnaker	53.1 (19.1 16.1 17.9)	35638	47.1 (13.1 16.2 17.7)	25831	50.0 (19.6 16.1 14.3)	16109	45.9 (13.7 15.7 16.4)	21111
artimon	46.9 (16.9 16.3 13.7)	34118	42.6 (13.5 15.2 13.9)	31216	40.8 (14.8 12.9 13.1)	21776	39.8 (12.7 12.1 15.0)	26681
soyotte	0.0 (0.0 0.0 0.0)	0	4.7 (4.2 0.5 0.0)	3934	4.6 (0.8 1.7 2.0)	11359	7.0 (4.8 2.1 0.1)	7652
fonck	0.0 (0.0 0.0 0.0)	0	5.6 (5.2 0.5 0.0)	4455	4.6 (0.8 1.7 2.2)	11763	7.3 (4.7 2.5 0.1)	7918
total sumflow		69756		65436		61007		63362
experiment 4								
spinnaker	53.9 (20.4 16.0 17.6)	36461	47.7 (14.5 15.0 18.2)	29249	49.6 (19.4 14.8 15.4)	18400	45.7 (14.3 13.9 17.6)	22822
artimon	46.1 (16.8 13.8 15.4)	33948	41.9 (12.7 14.4 14.8)	29770	41.4 (16.2 12.4 12.8)	20300	39.4 (12.3 11.9 15.2)	24971
soyotte	0.0 (0.0 0.0 0.0)	0	4.6 (4.4 0.2 0.0)	3517	4.5 (0.8 1.5 2.2)	11136	7.3 (5.3 2.0 0.1)	7877
fonck	0.0 (0.0 0.0 0.0)	0	5.8 (5.6 0.1 0.0)	4231	4.5 (0.8 1.1 2.6)	11367	7.5 (5.4 2.0 0.1)	8001
total sumflow		70409		66767		61203		63671
MEAN								
spinnaker	53.6 (18.5 16.5 18.6)	36932	47.5 (12.7 15.9 18.9)	27644	49.5 (18.1 15.2 16.2)	17270	45.9 (13.1 14.7 18.1)	21782
artimon	46.4 (15.9 14.8 15.7)	34630	42.3 (12.4 14.4 15.5)	31800	41.4 (14.9 13.0 13.5)	21716	39.7 (11.7 12.1 15.9)	26822
soyotte	0.0 (0.0 0.0 0.0)	0	4.7 (4.1 0.6 0.0)	3766	4.5 (0.7 1.5 2.3)	11522	7.0 (4.7 2.1 0.2)	7852
fonck	0.0 (0.0 0.0 0.0)	0	5.6 (5.2 0.4 0.0)	4346	4.6 (0.7 1.5 2.4)	11729	7.4 (5.0 2.3 0.2)	8198
total sumflow		71562		67556		62239		64654

Table 20. Scenario (c): processors utilization

Table 20 gives, for each experiment and each heuristic, the percentage of allocated tasks on the 500 of the experiment per server (the part of each task type is also specified in parenthesis), the sumflow per server and the total sumflow that has cost the execution of the whole experiment on the system.

	makespan			sumflow		
	HMCT	MP	MSF	HMCT	MP	MSF
experiment 1	5.5	13.3	9.7	5.6	13.4	9.9
experiment 2	5.4	13.0	9.8	5.4	13.2	9.9
experiment 3	6.1	12.4	9.0	6.2	12.6	9.1
experiment 4	5.1	13.0	9.5	5.1	13.1	9.6
MEAN	5.5	12.9	9.5	5.6	13.1	9.6

Table 21. Scenario (c): average percentage gain against MCT on the makespan and the sumflow for each client

Finally, Table 21 gives for each experiment and each heuristic, the average percentage that each application gains on the makespan and on the sumflow against if scheduled with MCT. One should note that gains on the sumflow that can be red in this table are close to those on the makespan (as expected), and of course, can differ from the one that can be computed from Table 20 where they would be gains on the whole experiment, e.g. experiment resource consumption benefices.

At first, we can note that MCT does not, or hardly, use the slowest servers (Table 20). This can lead to high contention on the fastest servers and delay the termination date of each tasks, then the makespan of each application. In fact, for each experiment, using the HTM leads to better performances and each application finishes sooner than when MCT schedules the experiment. MP seems to be the heuristic that leads to the best results, whatever metric is regarded : makespan, sumflow, average gain, but MP has also a considerable standard deviation, and a greater number of run has not proven to reduce it (mainly due to the use of the slowest servers, as it is explained below).

Indeed, whichever experiment MP schedules, it leads to better performances on the makespan and on the sumflow: a greater number of application finish sooner than when the experiment is scheduled with another heuristic, the average gain on the makespan (and so for the sumflow) for each application is around 13% against MCT, compared to 5% for HMCT and 9% for MSF (Table 21).

MP uses the slowest servers for the longest tasks, as opposed to MSF (Table 20) which tends to use the slowest for short tasks. We can also note that MP allocates less tasks to the slowest servers than the other, but as longest tasks cost the most, it leads to a greater sumflow on these servers and a lesser on the fastest.

The standard deviation on the makespan grows with the quantity of tasks mapped on the slowest servers and their type: MCT has a low standard deviation, HMCT a small one. It uses slow server, but for short tasks. MSF uses them also for tasks of second type and consequently its client makespan has a bigger standard deviation. MP has the biggest, using them mainly for long tasks.

Using the HTM leads to a better use of the system resources: the experiment sumflow is always inferior than MCT's (more than 13% if MP is used). Moreover, If we consider that each resource has a proportional cost to its power, then our heuristics, especially MP, would make an financial profit of much more than 13% because less expensive resources are the most solicited.

But, one should note that the utilization of resources with our heuristics can be sub-optimal: when only one application subsists (e.g. only sequential jobs remain), we have observed that our heuristics do not necessarily use the fastest server, due to the model/reality synchronization.

5.4. Scenario (d): Submission of 10 1D-mesh Application, Each Composed of a Variable Number of Wastecpu Tasks

This work is really close to the one of the previous section. We have undertaken it under the assumption that applications could be too homogeneous, and that this could interfere with general results.

All the parameters are the same as above, except for applications themselves, whose size is drawn uniformly between 20 and 80 for each application composing one of the four experiments. Hence, one can generate 3^n different applications per client, if n is the number of tasks drawn for the client. The composition of all the applications (numbers of tasks of each type and sizes of applications) for each experiment is given in Table 22. As before, one experiment has been executed at least 6 times.

The heterogeneity coefficient of the platform is equal to 8.9 and the testbed resources are:

- client: zanzibar ;
- agent: xrousse ;
- servers: spinnaker, artimon, soyotte, fonck.

client	experiment 1				experiment 2				experiment 3				experiment 4			
	type 1	type 2	type 3	**total**	type 1	type 2	type 3	**total**	type 1	type 2	type 3	**total**	type 1	type 2	type 3	**total**
client 1	23	22	31	**76**	17	21	17	**55**	13	5	7	**25**	5	10	9	**24**
client 2	18	19	23	**60**	15	26	24	**65**	12	6	7	**25**	17	13	15	**45**
client 3	18	17	18	**53**	19	28	25	**72**	13	7	10	**30**	11	8	5	**24**
client 4	24	17	22	**63**	25	20	23	**68**	15	19	16	**50**	10	8	5	**23**
client 5	26	19	21	**66**	14	9	15	**38**	13	6	19	**38**	30	23	22	**75**
client 6	23	27	21	**71**	14	15	12	**41**	19	18	16	**53**	16	19	26	**61**
client 7	29	20	29	**78**	12	16	23	**51**	11	13	17	**41**	28	17	28	**73**
client 8	19	8	10	**37**	10	11	12	**33**	10	4	9	**23**	20	26	12	**58**
client 9	29	16	15	**60**	27	24	23	**74**	14	23	19	**56**	20	33	21	**74**
client 10	19	17	29	**65**	10	7	11	**28**	14	15	15	**44**	11	14	17	**42**
total	228	182	219	**629**	163	177	185	**525**	134	116	135	**385**	168	171	160	**499**

Table 22. Scenario (d): applications composition

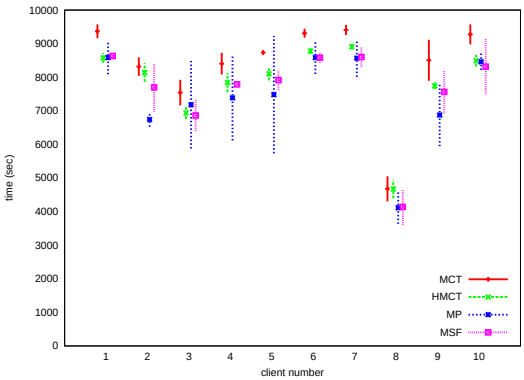

Figure 11. Scenario (d): results on the makespan for the first experiment

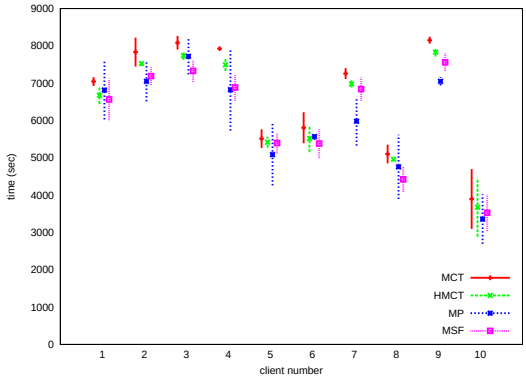

Figure 12. Scenario (d): results on the makespan for the second experiment

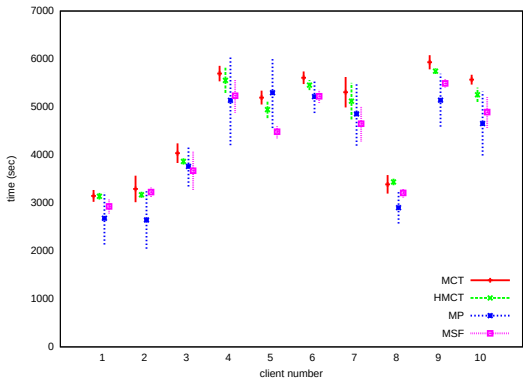

Figure 13. Scenario (d): results on the makespan for the third experiment

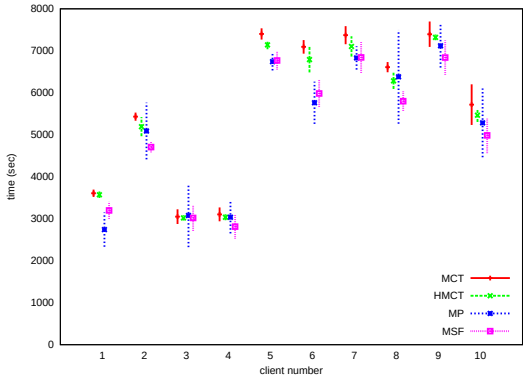

Figure 14. Scenario (d): results on the makespan for the fourth experiment

5.4.1 Results

Results of the 4 experiments are given in Figures 11, 12, 13, 14 and in Tables 23 and 24.

One can see in each graph the mean and the standard deviation of the makespan obtained on the 6 runs of each of the 10 submitted applications. Like explained in the previous section, since applications are 1D-mesh, graphs

of application sumflows are nearly identical to those for the makespan. Then, commentaries on applications makespans are valid for applications sumflows.

Table 23 gives, for each experiment and each heuristic: the percentage per server of allocated tasks (the percentage per type is also specified in parenthesis) on the number of tasks of the given experiment (which is given in Table 22) ; the sumflow per server and the total sumflow that has cost the whole experiment on the system.

At last, Table 24 gives the average percentage gain that each application gains on the makespan and on the sumflow if scheduled with our heuristics against MCT.

experiment 1								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	53.6 (18.8 15.7 19.1)	43246	47.8 (13.9 14.0 19.9)	31757	50.2 (18.7 15.1 16.5)	20456	44.7 (13.0 13.5 18.2)	24223
artimon	46.4 (17.4 13.3 15.7)	38815	40.5 (12.0 13.9 14.6)	34357	40.5 (15.3 11.6 13.7)	24129	40.9 (14.5 10.9 15.5)	28759
soyotte	0.0 (0.0 0.0 0.0)	0	5.3 (4.5 0.6 0.2)	5374	4.6 (1.2 0.9 2.5)	14770	7.1 (4.6 2.0 0.5)	10544
fonck	0.0 (0.0 0.0 0.0)	0	6.4 (5.9 0.4 0.1)	6103	4.6 (1.1 1.4 2.1)	14001	7.4 (4.2 2.5 0.6)	11477
total sumflow		82061		77591		73356		75003
experiment 2								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	54.5 (17.0 18.4 19.0)	35248	49.1 (13.1 16.7 19.3)	28022	50.5 (16.4 17.5 16.6)	17733	46.3 (10.8 16.9 18.7)	22008
artimon	45.5 (14.0 15.3 16.2)	31211	42.4 (9.8 16.7 15.9)	29492	41.6 (14.0 13.6 14.0)	20934	39.5 (10.6 12.7 16.3)	23671
soyotte	0.0 (0.0 0.0 0.0)	0	3.5 (3.5 0.0 0.0)	2474	3.4 (0.0 1.0 2.5)	9557	7.0 (4.7 2.2 0.1)	7420
fonck	0.0 (0.0 0.0 0.0)	0	5.0 (4.6 0.4 0.0)	3665	4.5 (0.7 1.6 2.2)	11375	7.2 (5.0 2.0 0.2)	7486
total sumflow		66459		63653		59599		60585
experiment 3								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	54.4 (19.7 16.2 18.4)	24492	51.2 (16.2 16.1 18.8)	20973	49.7 (18.1 14.9 16.8)	13027	46.5 (13.8 13.8 19.0)	15796
artimon	45.6 (15.1 13.9 16.6)	22175	44.3 (14.0 14.0 16.2)	21776	41.3 (15.6 12.1 13.6)	13389	38.4 (9.0 13.4 16.1)	16904
soyotte	0.0 (0.0 0.0 0.0)	0	1.4 (1.4 0.0 0.0)	708	4.5 (0.6 1.8 2.1)	7631	7.3 (5.8 1.4 0.0)	4648
fonck	0.0 (0.0 0.0 0.0)	0	3.1 (3.1 0.0 0.0)	1537	4.4 (0.5 1.3 2.6)	7566	7.8 (6.2 1.6 0.0)	5026
total sumflow		46667		44994		41613		42374
experiment 4								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	54.7 (19.0 19.0 16.6)	30543	48.9 (13.5 17.5 17.8)	24356	49.2 (17.8 16.2 15.1)	15402	46.3 (12.6 15.9 17.7)	18488
artimon	45.3 (14.6 15.2 15.4)	25555	43.8 (12.8 16.7 14.2)	25334	41.7 (14.8 14.0 12.8)	16013	40.6 (11.8 14.5 14.2)	19653
soyotte	0.0 (0.0 0.0 0.0)	0	2.7 (2.7 0.0 0.0)	1750	4.5 (0.5 1.9 2.1)	9848	6.0 (4.0 1.9 0.1)	5725
fonck	0.0 (0.0 0.0 0.0)	0	4.6 (4.6 0.0 0.0)	2978	4.6 (0.5 2.1 2.0)	10226	7.1 (5.2 1.9 0.0)	6462
total sumflow		56098		54418		51489		50328
MEAN								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	54.3 (18.7 17.3 18.3)	33382	49.2 (14.2 16.1 19.0)	26277	49.9 (17.7 15.9 16.2)	16654	45.9 (12.5 15.0 18.4)	20129
artimon	45.7 (15.3 14.4 16.0)	29439	42.7 (12.2 15.3 15.2)	27740	41.3 (14.9 12.8 13.5)	18616	39.9 (11.5 12.9 15.5)	22247
soyotte	0.0 (0.0 0.0 0.0)	0	3.2 (3.0 0.2 0.1)	2576	4.3 (0.6 1.4 2.3)	10452	6.8 (4.8 1.9 0.2)	7084
fonck	0.0 (0.0 0.0 0.0)	0	4.8 (4.5 0.2 0.0)	3571	4.5 (0.7 1.6 2.2)	10792	7.4 (5.2 2.0 0.2)	7613
total sumflow		62821		60164		56514		57072

Table 23. Scenario (d): processors utilization

Same conclusions than in the previous section can be made here, even if sizes of applications are different from each other. MCT does not use any of the SUN servers because of their slow computation power, and gives the worst results whatever the considered metric is. This was expectable: because applications costs are more heterogeneous that before, the throughput is not constantly high. MCT has even less the need of slower servers.

Using MP is not as good as before, but is still the best on average regardless the metric (even slightly against MSF). One can also note that the standard deviation is smaller for all heuristics and especially for MP, although servers utilization is quiet identical: the lower throughput hence the lower contention on servers is the reason that explains these two facts.

Indeed, we can observe in Table 23 the same behaviour of the heuristics than in the previous section. MP mappes longer tasks to slower servers, HMCT uses them only to compute short tasks, and MSF avoids to allocate

	makespan			sumflow		
	HMCT	MP	MSF	HMCT	MP	MSF
experiment 1	5.7	10.5	9.4	5.2	10.8	8.9
experiment 2	4.0	10.1	8.8	4.1	10.3	8.9
experiment 3	3.4	11.0	8.7	3.5	11.2	8.9
experiment 4	2.7	8.4	9.7	2.8	8.5	9.8
MEAN	4.0	10.0	9.1	3.9	10.2	9.1

Table 24. Scenario (d): average percentage gain against MCT on the makespan and the sumflow for each client

longer tasks on them . MP allocates less tasks to the slowest servers, but as MP uses them to compute costliest tasks, they compute for a larger amount of time than when used with the other scheduling heuristics. Nonetheless, due to less contention, two runs will not much differ.

Performances on the average gain on the makespan are smaller than in the previous section, but the gain for each application is around 10% for MP and MSF (Table 24).

Using the HTM leads to better performances on the resources utilization: on average, an experiment requires 10% less resources if scheduled with MP or MSF than with MCT. Morevover, if a proportional cost to the server power is applied, MP leads to the cheapest schedules observed here. Indeed, if experiment sumflows of MP and MSF are tight, MP uses more slower servers and less faster than MSF.

5.5. Scenario (e): Submission of 250 Independent Tasks Concurrently to 5 1D-mesh Applications, Each Composed of 50 Wastecpu Tasks

We propose here to study the behavior of the heuristics in a more general frame, that we expect to be closer to the real world. Therefore, 250 independent tasks are launched during the submission by 5 clients of a 1D-mesh of size 50. In the following, we envisage that the set of independent tasks can be submitted by one unique client (then comparison between two set sumflows are relevant) and that each task can be submitted by a different client (then task duration gains comparisons are valuable information). In consequence, the agent deals with at least 6 clients.

There is 255 arrival dates to determine : 250 for independent tasks and 5 for head arrival dates of 1D-mesh applications. The difference between two arrival date is drawn from a Poisson distribution with the parameter $\mu = 20$. The position of the client's head in the 255 arrival dates is drawn with a Uniform distribution. The position of the head arrival date is also called its *indice* or *client number*. All other parameters are the same than in previous sections.

In these sets of experiments, depending of the heuristic, the system can exceptionnally have to deal with more than 10 tasks at a time in the system, on the contrary of previous 1D-mesh experiments. Throughput is not constant thus implying load fluctuations.

Four sets of at least six runs have been executed, two sets differing from each other in arrival dates, clients' indices which are given in the corresponding 'makespan and sumflow results' figures and applications compositions which are given in Table 25.

The heterogeneity coefficient of the platform is still equal to 8.9 and the testing platform is again composed of:

- client: zanzibar ;

- agent: xrousse ;
- servers: spinnaker, artimon, soyotte, fonck.

client	experiment 1			experiment 2			experiment 3			experiment 4		
	type 1	type 2	type 3	type 1	type 2	type 3	type 1	type 2	type 3	type 1	type 2	type 3
client 1	17	20	13	12	18	20	17	11	22	20	21	9
client 2	18	12	20	13	19	18	12	20	18	16	14	20
client 3	18	18	14	16	15	19	9	26	15	15	16	19
client 4	11	20	19	18	15	17	14	17	19	16	18	16
client 5	22	9	19	15	13	22	14	20	16	18	18	14
metatask	92	72	86	93	83	74	80	84	86	81	85	84
total	178	151	171	167	163	170	146	178	176	166	172	162

Table 25. Scenario (e): Applications Composition

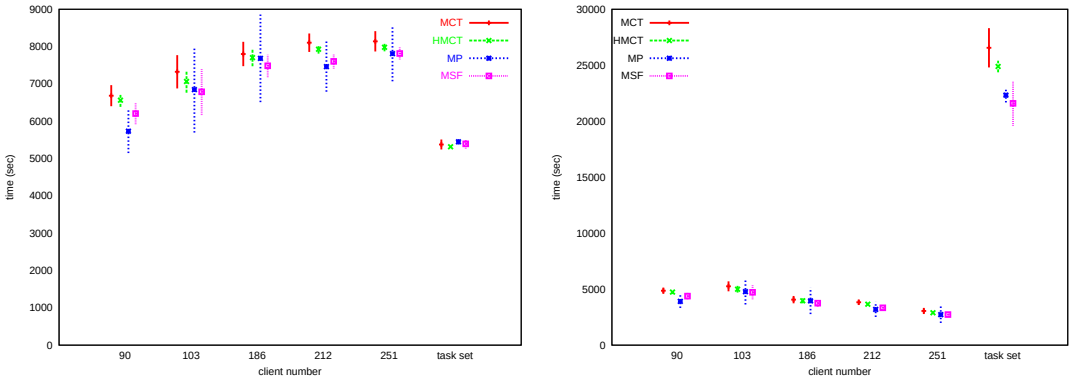

Figure 15. Scenario (e): Results on the Makespan and on the Sumflow for the First Experiment

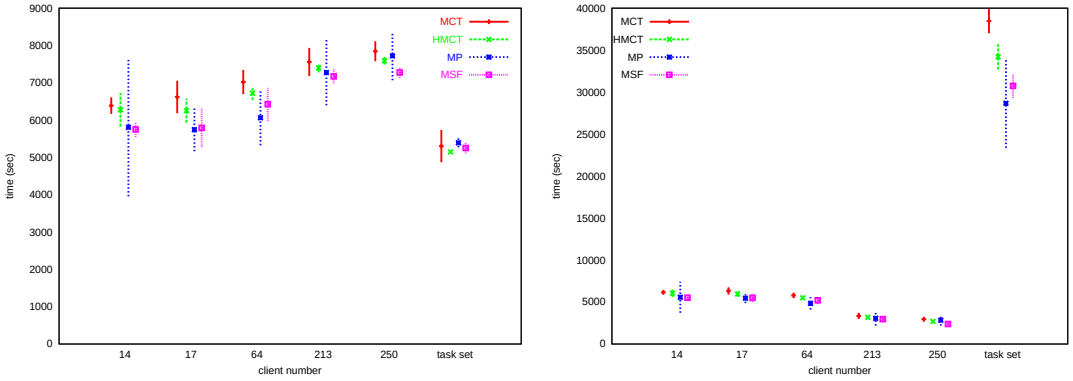

Figure 16. Scenario (e): Results on the Makespan and on the Sumflow for the Second Experiment

5.5.1 Results

There are several things to look at in this section: results for each of the 5 clients and of the metatask on metrics like the makespan, the sumflow, but we can also consider the quality of service given to each task of the metatask.

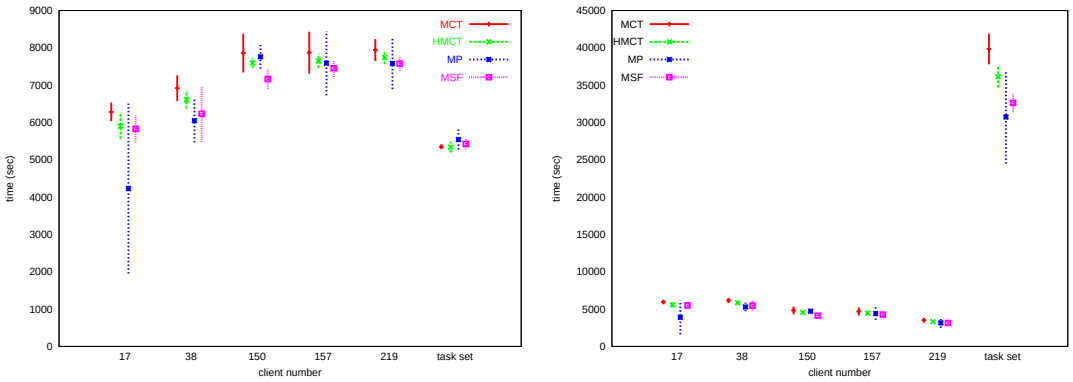

Figure 17. Scenario (e): Results on the Makespan and on the Sumflow for the Third Experiment

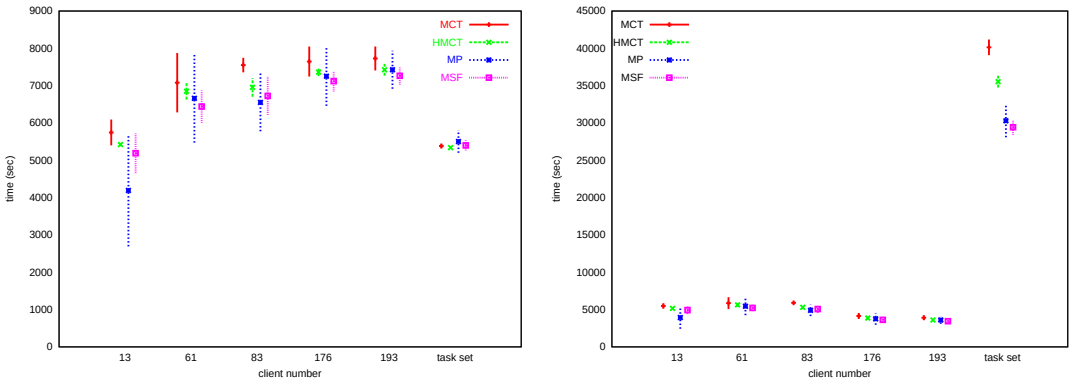

Figure 18. Scenario (e): Results on the Makespan and on the Sumflow for the Fourth Experiment

Then, one can see the results of the 4 subsets of experiment resumed in Figures 15, 16, 17, 18 and in Tables 26, 27, 28 and 29.

As noted in previous sections, with 1D-mesh applications, the makespan value is the sumflow value added to the application head arrival date. But, on the opposite of previous sections, head arrival dates are not negligible as the head indices get greater. For example, because in this section $\mu = 20$, an application with an indice around 200 begins at a time around 4000 seconds. Morevover, we deal here with the submission of a set of independent tasks.

We can see in Figures 15, 16, 17, 18 the makespan on the left hand and the sumflow on the right hand of all applications including the set of independent tasks. For this set, the makespan is quiet constant among the heuristics, and we have shown this to be expected. MP can have a great standard deviation on the makespan of the 1D-meshes, but presents this characteristic on the sumflow of the set of independent taks too.

Concerning the gain for **each** 1D-mesh client on the makespan and on the sumflow against if the experiment is scheduled with MCT, one can see in Table 27 that using our heuristics leads to better gains, but more precisely, that MP and MSF realize on average a 9.3% and 7.5% benefit on the makespan respectively, and a 12.4% and 11.4% benefit on the sumflow. In fact, MP achieves to minimise the makespan **and** the sumflow on the average. Results obtained for the set of tasks on the sumflow is nearly the twice than for a client: MP minimises the sumflow with a 22% gain and MSF achieves similar performances with 20.6%.

experiment 1								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	55.2 (19.4 16.8 19.0)	25676	54.3 (18.8 16.8 18.7)	22159	52.6 (20.2 15.2 17.2)	14057	52.4 (18.4 16.0 17.9)	17014
artimon	44.7 (16.1 13.3 15.2)	21781	43.8 (14.9 13.4 15.5)	21743	38.0 (12.7 12.0 13.3)	12059	39.2 (10.5 12.4 16.3)	16460
soyotte	0.0 (0.0 0.0 0.0)	0	0.6 (0.6 0.0 0.0)	413	4.4 (1.0 1.7 1.7)	7112	3.8 (2.9 0.9 0.0)	3251
fonck	0.2 (0.1 0.0 0.0)	173	1.3 (1.3 0.0 0.0)	833	5.0 (1.8 1.3 2.0)	7659	4.6 (3.8 0.8 0.0)	3781
total sumflow		47630		45148		40887		40506
experiment 2								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	54.2 (17.9 18.4 17.9)	31848	50.7 (14.8 17.6 18.2)	30368	53.0 (19.6 16.0 17.4)	18888	48.2 (13.6 16.7 17.9)	24095
artimon	45.3 (15.2 14.2 15.9)	30428	44.2 (13.5 14.9 15.8)	23818	37.8 (11.8 12.8 13.2)	14495	41.0 (11.5 13.6 15.9)	18074
soyotte	0.2 (0.1 0.0 0.1)	491	2.1 (2.0 0.0 0.0)	1415	4.2 (0.7 1.8 1.7)	8152	5.5 (4.3 1.2 0.0)	5096
fonck	0.2 (0.1 0.0 0.1)	270	3.0 (3.0 0.0 0.0)	1988	5.0 (1.3 2.0 1.8)	8886	5.4 (4.0 1.2 0.2)	5033
total sumflow		63037		57589		50421		52298
experiment 3								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	54.1 (15.5 19.8 18.8)	33579	51.5 (14.0 19.2 18.3)	27253	50.9 (16.6 17.6 16.8)	17259	49.2 (12.6 17.8 18.8)	21923
artimon	45.0 (13.5 15.6 16.0)	29834	42.6 (9.8 15.8 16.9)	28110	39.6 (11.3 14.0 14.3)	16610	41.2 (10.4 14.5 16.3)	22291
soyotte	0.4 (0.1 0.1 0.2)	487	2.6 (2.3 0.3 0.0)	1947	4.5 (0.6 1.8 2.0)	8680	4.6 (2.9 1.7 0.0)	5306
fonck	0.5 (0.1 0.1 0.3)	1083	3.4 (3.1 0.3 0.0)	2591	5.0 (0.7 2.2 2.1)	9646	5.0 (3.3 1.6 0.1)	5640
total sumflow		64983		59901		52195		55160
experiment 4								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	54.7 (17.9 19.3 17.5)	33797	50.1 (13.8 19.1 17.2)	25791	49.9 (17.4 16.1 16.5)	16607	48.1 (13.2 17.2 17.8)	19589
artimon	45.1 (15.1 15.0 14.9)	31432	42.9 (12.7 15.0 15.2)	28330	40.6 (14.1 14.5 12.0)	17104	41.1 (12.6 14.0 14.5)	21034
soyotte	0.2 (0.1 0.0 0.0)	129	3.0 (2.9 0.1 0.0)	2091	4.4 (0.4 2.1 1.8)	8814	5.2 (3.6 1.6 0.0)	5391
fonck	0.1 (0.0 0.0 0.0)	77	4.0 (3.8 0.2 0.0)	2888	5.1 (1.3 1.7 2.1)	9407	5.6 (3.8 1.6 0.1)	5715
total sumflow		65435		59100		51932		51729
MEAN								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	54.5 (17.7 18.6 18.3)	31225	51.6 (15.4 18.2 18.1)	26393	51.6 (18.5 16.2 16.9)	16703	49.5 (14.4 16.9 18.1)	20655
artimon	45.0 (15.0 14.5 15.5)	28369	43.4 (12.7 14.8 15.8)	25500	39.0 (12.4 13.3 13.2)	15067	40.6 (11.2 13.6 15.8)	19465
soyotte	0.2 (0.1 0.0 0.1)	277	2.1 (2.0 0.1 0.0)	1466	4.4 (0.7 1.9 1.8)	8190	4.8 (3.4 1.3 0.0)	4761
fonck	0.2 (0.1 0.1 0.1)	401	2.9 (2.8 0.1 0.0)	2075	5.1 (1.3 1.8 2.0)	8900	5.1 (3.7 1.3 0.1)	5042
total sumflow		60271		55434		48859		49923

Table 26. Scenario (e): Processors Utilization

	1D-mesh clients						METATASK		
	makespan			sumflow			sumflow		
	HMCT	MP	MSF	HMCT	MP	MSF	HMCT	MP	MSF
experiment 1	2.1	6.8	5.7	3.9	11.8	10.3	6.3	15.9	18.7
experiment 2	3.4	8.3	8.7	5.2	10.5	12.9	10.5	24.3	19.9
experiment 3	3.8	10.9	7.2	5.4	13.4	10.5	9.5	23.1	18.4
experiment 4	4.9	11.0	8.5	6.9	13.9	11.9	11.1	24.3	25.1
MEAN	3.6	9.3	7.5	5.4	12.4	11.4	9.4	21.9	20.6

Table 27. Scenario (e): Average Percentage Gain against MCT on the Makespan and the Sumflow for Each Client

In Tables 29 and 28, we note the better quality of service of all of our heuristics. The percentage of tasks that finish sooner than MCT in Table 29 has been computed like explained previously (in a 'cross-product' fashion, mean of $6 * 6 = 36$ tests that has been performed). The number in parenthesis is the performance of MCT and the difference between the sum of the two number to 100 is the percentage of tasks finishing around 1 second of the same date, thus said to "finish at the same date".

		mean flow	gain in percentage		
		MCT (sec)	HMCT	MP	MSF
	type 1	53.4	1.0	21.7	0.6
experiment 1	type 2	104.0	10.9	17.7	19.0
	type 3	164.6	5.7	13.0	24.8
	type 1	77.9	-0.6	29.5	-6.0
experiment 2	type 2	160.9	12.1	17.2	20.2
	type 3	241.3	15.0	30.0	30.6
	type 1	76.7	-2.9	32.5	-7.4
experiment 3	type 2	151.4	11.9	14.7	12.7
	type 3	244.2	11.3	25.0	28.8
	type 1	80.0	-1.9	31.9	4.5
experiment 4	type 2	170.1	15.6	20.2	27.4
	type 3	228.5	12.8	25.3	33.6
MEAN	-	146.1	7.6	23.2	15.7

Table 28. Scenario (e): Average Percentage Gain for $\mu = 20$ sec on Each Task Given by Type

We can see that our heuristics lead always to more tasks that finish soonner, and bests results are obtained for MP which achieves to place 80% of tasks that finish sooner than if scheduled with MCT. Still on the average, 5% of tasks finish 'at the same date'. Nonetheless, neither MP nor MSF beat MCT on the maxtretch, e.g. the worst case delay proportionnally to the time a task requires on the same server. Still, MCT beats MP on the maxflow, but MSF performs better (and HMCT even better).

To confirm the quality of the previous results, one can see in Table 28, for each type of task and each experiment, the mean flow obtained when the task has been scheduled with MCT. On the same line is given the percentage of gain on the duration of the task when the experiment is scheduled with the given heuristic.

Each independent task is 23% or 15.7% shorter if using MP or MSF. One can also note that using the HTM with HMCT lead to improve the scheduling: better quality of service and better makespan and sumflow regardless the client.

At last, one can see the experiments cost with the detailed sumflow values in Table 26. Our heuristics give better results, and MP beats the other on the average. We can observe that MP uses slower servers to preferably scheduled average and long duration tasks (type 2 and 3). This leads to higher sumflows on slowest servers even if less tasks than with MSF are mapped on them. On the opposite, HMCT and MSF compute a larger part of type 1 tasks on them than other type. The heuristic behavior is identical to the one that has been observed in previous scenarios.

Finally, on a financial point of vue, as faster servers usage costs normally more than slower ones, MP minimises the cost of the experiment. Because tasks that are mapped to slower servers are at least of average duration, the time required on these servers can be considered as huge against MCT's (8900 seconds on fonck for MP against 401 seconds for MCT in average), but also cheaper than the cost of the difference between the sumflow utilized on faster servers (16703 seconds on spinnaker for MP against 31225 seconds for MCT, hence half the cost).

	NetSolve's MCT					HMCT					MP					MSF				
	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**
makespan	5377	5302	5350	5383	**5353**	5315	5148	5337	5340	**5285**	5448	5393	5544	5505	**5472**	5393	5254	5429	5399	**5369**
sumflow	26559	38461	39850	40133	**36251**	24888	34204	36138	35534	**32691**	22333	28669	30732	30294	**28007**	21594	30739	32649	29435	**28604**
maxflow	363.2	464.9	561.0	397.4	**446.6**	312.8	303.3	381.9	331.0	**332.2**	549.2	658.5	656.5	651.3	**628.9**	318.4	409.3	454.0	395.1	**394.2**
maxstretch	11.0	11.7	13.8	10.0	**11.6**	9.1	11.2	13.3	11.7	**11.4**	14.7	17.1	17.8	18.3	**17.0**	13.5	16.2	18.3	17.2	**16.3**
percentage of tasks that finish sooner than with MCT	-	-	-	-	–	53 (34)	61 (36)	62 (34)	64 (32)	**60(34)**	72 (16)	85 (14)	82 (15)	83 (14)	**80(15)**	65 (22)	71 (26)	72 (25)	76 (21)	**71(24)**

Table 29. Scenario (e) :Results in Seconds for $\mu = 20$ sec on Wastecpu Tasks

5.6. Scenarios (f,g,h,i,j): Submissions Containing a Stencil Application

The kernel of a stencil application is given in Figure 6. Each of its tasks have same needs, and so require the same amount of time. We present in this section different scenarios: submissions of a stencil application composed of tasks of type 1 then of type 3 ; submissions of a stencil application in parallel of a independent tasks submitted at two different rates and finally the submission of a smaller stencil graph concurrently to independent tasks.

Firstly, we point on some remarks on the common experiments background.

5.6.1 Notes

Relying on [BBR01], a stencil application in this work is composed of one type of task. It is composed of 10 or 5 tasks width and the depth of the graph is also given in the corresponding subsection (50 for the first, 25 for the other).

When a client begins to request the agent for its stencil, *w*idth tasks are submitted. If no independent task is submitted in parallel, a maximum of *w*idth tasks can be present in the system at a time. In the following, and as written in Figure 6, we refer by the task (i,j) to the task which is on the *ith* line and *jth* column.

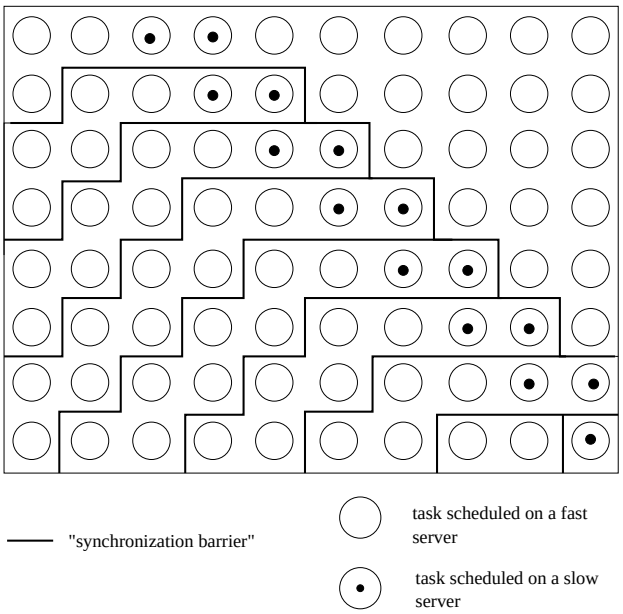

Figure 19. Example of a 10x8 stencil application execution

The agent can have to theorically face a set of requests (10 at the beginning of the submission for example). But in reality, the agent receives them in a given order. There are two remarks to do on that point: firstly, the submission is implementation dependant. That means that the client can try to force tasks that are higher in the graph to be submitted first in the pool of the ready tasks (tasks are submitted in a "lexical order" with the (i,j) information) but other submission orders can be made. We have chosen the first implementation. Second, because of the client system (scheduling of threads and fork processes) or network problems (congestion), requests can be validated by the agent in a different order than the one wanted by the client. Due to the experimental platform, we do not have this problem in this work.

One should be cautious considering the results: we recall that the agent has no information on the applications it has to schedule. Furthermore, as one can see, this kind of graph is *a priori* a good counter-example for the makespan of the good behavior of MP in general and is done on purpose. Indeed, Figure 19 shows a MP schedule of a 10*8 stencil application on a hypothetical testbed composed of 2 same fast servers and 2 same slow servers,

with the hypothesis that the heterogeneity coefficient is at least 13 (e.g. that task duration on a slow server is at least 13 times superior to its duration on a fast one). Tasks that are assigned to slow servers are marked with a dot in their center.

This example shows the main drawback of MP, that we have already explained in [CJ02]: if there are idle servers left in the system, MP chooses them to place the task. It can also use them if the perturbation is too high on the fastest servers, even if it is due to tasks that will finish in a few seconds and let the fast server idle. We will see the effect of this scheduling strategy.

Indeed, one can easily see boundaries where faster servers are idle and wait for the ending of tasks mapped to slower ones. These boudaries give a *synchronization barrier effect*, and in our case, it is easy to show that they are of the same number than the depth of the graph. So MP is particularly targeted with that kind of kernel.

In the following sections, we have an heterogeneity of 8.9, and the testing environment is made with the following servers:

- client: zanzibar ;
- agent: xrousse ;
- servers: spinnaker, artimon, soyotte, fonck.

5.6.2 Scenarios (f) and (g): Submission a Stencil Applications, Consequences of the Task Type

We consider in this section 2 submissions of a 10*50 stencil application: the first one composed of tasks of type 1 and the second of tasks of type 3.

Scenario (f): 10*50 Stencil Composed of Tasks of Type 1
The type of task involved in this scenario is the first one: the stencil is only made of the shortest duration task type (tasks durations are given in Table 5).

Makespan and sumflow graphs are given in Figure 20 and the detailed sumflow per server can be found in Table 30.

One can see that MP gives a higher makespan than MCT but minimises the sumflow: this is explained later. MSF minimises the makespan and behaves the same along the runs: the standard deviation for the makespan is very low. It outperforms MCT with nearly half the sumflow.

We can also see the different behavior of MCT which uses more artimon than spinnaker (see Table 30. This is mainly because of the lack of precision of task durations which are computed with the load average sent by the servers and corrected by the load correction mechanisms. On the opposite, HMCT which uses slower servers behaves like usual when there is perturbation.

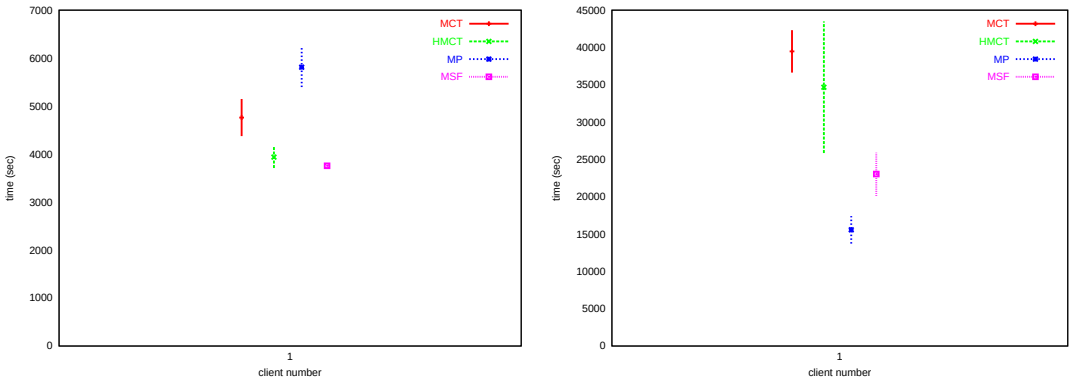

Figure 20. Scenario (f): makespan and sumflow results

server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	43.3 (43.3 0.0 0.0)	12383	53.3 (53.3 0.0 0.0)	18183	66.6 (66.6 0.0 0.0)	5720	50.6 (50.6 0.0 0.0)	10160
artimon	56.7 (56.7 0.0 0.0)	27094	46.0 (46.0 0.0 0.0)	16065	22.2 (22.2 0.0 0.0)	2533	43.9 (43.9 0.0 0.0)	9375
soyotte	0.0 (0.0 0.0 0.0)	0	0.2 (0.2 0.0 0.0)	150	2.3 (2.3 0.0 0.0)	1507	1.7 (1.7 0.0 0.0)	1115
fonck	0.0 (0.0 0.0 0.0)	0	0.4 (0.4 0.0 0.0)	278	9.0 (9.0 0.0 0.0)	5805	3.7 (3.7 0.0 0.0)	2391
sumflow		39477		34676		15565		23041

Table 30. Scenario (f): servers utilization

The remark done in section 5.6.1 about the execution of the stencil application if scheduled with MP is not exactly valid here, because of the heterogeneity coefficient of 8.9. But the same kind of thing happens here (see Figure 21):
Tasks (0,2) and (0,3) are allocated to fonck and soyotte, and artimon and spinnaker receive and execute all the tasks available until tasks (2,8) and (2,9). It is interesting to see that tasks (2,8) and (2,9) are allocated to fonck and soyotte, at time 119. It is surprising because these tasks have not yet finished, but the perturbation is minimum on these servers, and so tasks (0,2) and (0,3) are delayed in time. That's why the scheduled plan explained in section 5.6.1 is only valid on a system with a higher heterogeneity coefficient. When tasks (2,8) and (2,9) are assigned, there is no task left to submit to the agent until tasks (0,2) and (0,3) finish at time 141. Spinnaker and artimon finish their last tasks at time 134 and 136 respectively, then they are idle at least 5 seconds. Fonck and soyotte are chosen next to schedule tasks (3,2) and (3,3). All tasks until then are realized by the two fast servers. As before, tasks (2,8) and (2,9) were not finished, so they are delayed in time and finish finally at time 290. But, when task (4,5) finish at time 279, there is no work to do and all tasks previously assigned on the fast servers are done. Fast servers are idle 12 seconds. This confirms the remark about MP and its possible results on this type of kernel. But further works have to be done to conclude, because MP can still achieve an *a priori* good work in a multi-client system (see section 5.6.3).

This explains why MP achieves the worst makespan, but minimises the sumflow: there is less contention on fast servers thus the lower cost.

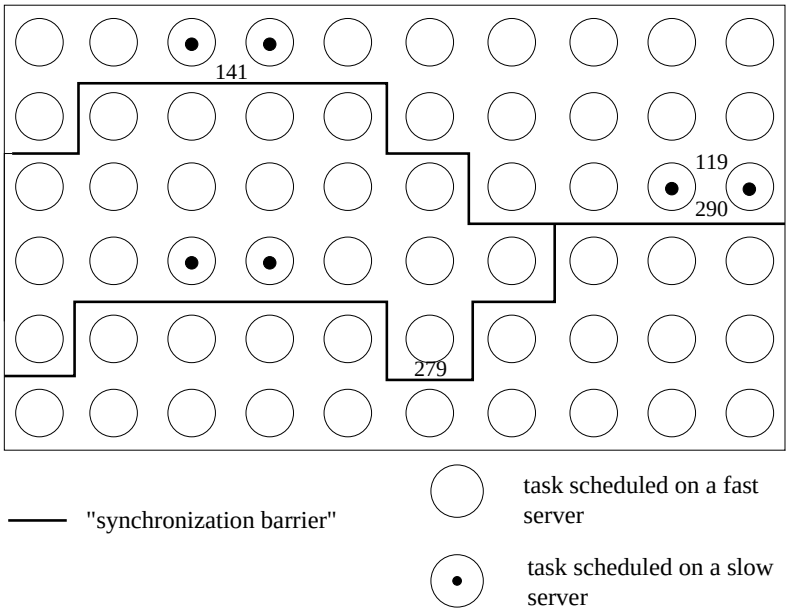

Figure 21. Scenario (f): schedule of MP

Scenario (g): 10*50 Stencil Composed of Tasks of Type 3
Because of the duration of a run, this subset is only composed of one run. The main objective was to confirm, and it does, expected behaviours of heuristics in their tendancies regarding each metric.

The graph of the application is still composed of 10 tasks width and 50 depth, but the task type is the longest one, e.g. tasks are of type 3 (see Table 5 for more details).

Makespan and sumflow graphs are given in Figure 22 and the server utilization where information like the sumflow and the percentage of tasks scheduled per server can be found is given in Table 31.

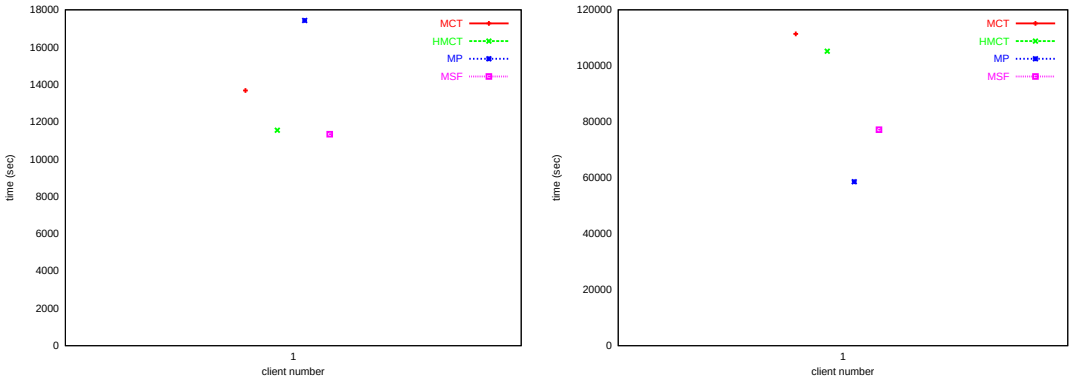

Figure 22. Scenario (g): makespan and sumflow results

server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	46.4 (0.0 0.0 46.4)	38633	53.4 (0.0 0.0 53.4)	53743	47.8 (0.0 0.0 47.8)	13481	51.6 (0.0 0.0 51.6)	35985
artimon	53.6 (0.0 0.0 53.6)	72776	46.6 (0.0 0.0 46.6)	51461	34.2 (0.0 0.0 34.2)	10498	45.0 (0.0 0.0 45.0)	34693
soyotte	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	9.0 (0.0 0.0 9.0)	17204	0.6 (0.0 0.0 0.6)	1150
fonck	0.0 (0.0 0.0 0.0)	0	0.0 (0.0 0.0 0.0)	0	9.0 (0.0 0.0 9.0)	17388	2.8 (0.0 0.0 2.8)	5343
sumflow		111409		105204		58571		77171

Table 31. Scenario (g): servers utilization

The results, if confirming the bad tendancies of MP on the makespan, are interesting for they show, on the opposite of the type 1 stencil where 66% of the tasks were assigned on spinnaker, that the slower servers are used. That means that, in this case, the "synchronization barrier effect" is radically minimized due to the duration of tasks. Indeed, the reason is the heterogeneity coefficient: 1 second of perturbation on slow servers can be seen as at least 8.9 seconds of perturbation on spinnaker.

Results
One can find a recapitulation of the gain realized by our heuristics against MCT on the makespan and the sumflow in Table 5.6.2. Results show that the utilization of the HTM brings a lot in the decision making, even if only one application is involved: the schedule is built on top of a higher knowledge of what is done on each server.

First, one should note the same aspect of graphs for these two scenarios: we find the same behavior on the makespan and on the sumflow for both scenarios.

As expected, MP does bad performances on the makespan, mainly due to the sub-utilization of fast servers (they are forced to stay idle and wait for slow servers to complete their tasks hence making new jobs to be available). On the opposite, MP has good performances on the sumflow. Of course, one should say that using sequentially the fastest server to execute tasks would do a bad makespan result and a good sumflow result, like MP does. Nevertheless, results in Tables 30 and 31 show that, if 66% of the tasks were effectively affected to spinnaker for the type 1, there is only 47.8% for the type 3 for same results characteristics.

MSF achieves to have good performances on both the makespan and the sumflow: it minimises the makespan for both experiments and its schedules requires near half the sumflow that MCT take for the same experiment.

HMCT gives as good preformances as MSF on the makespan, but the sumflow, even if less than MCT, is much greater than MSF's. This shows that for that kind of kernel, in a mono-client platform, HMCT which has the policy to minimize the completion date of the new query, achieves to make good results on the makespan but this also confirms that perturbations on previously assigned tasks has to be taken into account to minimise at the same time other metrics. Moreover, optimising other metrics does not mean degrading the makespan performance: MSF is definetely designed as a good trade-off between the makespan and the sumflow.

type **1**	HMCT	MP	MSF
makespan	17.3 %	-22 %	21.1 %
sumflow	12.2 %	60.6 %	41.6 %

type **3**	HMCT	MP	MSF
makespan	15.6 %	-27.4 %	17.1 %
sumflow	5.6 %	47.4 %	30.7 %

Table 32. Average gain on the makespan and the sumflow against MCT, when stencil is composed of tasks of type 1 or type 3

5.6.3 Scenarios (h) and (i): Submission of a 10*25 Stencil Application in Parallel of Independent Tasks

As explained in the previous section, further experiments in a multi-clients context is needed to see if heuristics behaviour is context dependent. In fact, we expect here better results for MP on the makespan, still the best results on the sumflow and good quality of service properties. Moreover, this scenario should confirm that MSF is a good trade-off between the makespan and the sumflow, and also that a good quality of service is given to each independent task.

In the folowing, stencil application are 10 tasks width wide, and have a depth of 25 tasks: they consist in 250 tasks. As we have seen in the previous section, at most 10 tasks were in the system at a given time. This is not true anymore since tasks of the metatask can be submitted to the agent.

Scenario (h) is instantiated with an inter-arrival rates for a set of 174 independent tasks drawn from a Poisson distribution with $\mu = 28$. Scenario (i) involves 'only' 87 tasks and the Poisson distribution uses $\mu = 45$ seconds. The number of independent tasks has been chosen so that the submission of the stencil begins and ends during the execution of some of them on the environment.

	type 1	type 2	type 3
experiment 1	66	49	59
experiment 2	67	49	58

Table 33. Scenario (h): independent tasks composition

Scenario (h)
We have conducted two experiments of three runs each. One experiment consists in the submission of 174 independent tasks, whose detailed composition is given in Table 5.6.3, and a 10*25 stencil application. In consequence, 424 tasks are submitted to the agent by two clients in a run.

The two experiments are generated with two different seeds to draw the arrival date of tasks of the independent tasks set and its composition. Then, even if the two sets have nearly the same composition (see Table 33), the order and arrival dates are different). The difference between two arrival dates is drawn from a Poisson distribution of mean equal here to $\mu = 28$ seconds, and a task has a Uniform probability to be of one task type.

One should be coutious when reading HMCT results: during the first experiment, some independent tasks *h*ave not been accepted by servers (tasks 35 and 53, 38 and 49, and 37 in respectively the first, second and third run). Moreover, in the second experiment, task 40 has been rejected in the first run. In the second run, task 48 and the 48th submitted task of the stencil have not been processed. In the third run, the 46th and 71th submitted task of the stencil have also been rejected. One must note that when a task is rejected by the environment, the task is considered as 'done' with a slightly nul duration. For independent tasks, this leads to an experiment with a lower resource consumption in regard to the other heuristics. But for a task involved in a stencil, that also means that some tasks may be in a *r*eady state before time.
Nonetheless, to have an idea of the HMCT results, we have used MCT results for the missing independent tasks and assumed that a missing stencil task have been mapped on spinnaker. HMCT is not able to handle the throughput of this scenario at a high rate, but comparisons between MP, MSF and MCT are of course valid.

Average makespan and sumflow (with their respective standard deviation) of submitted applications graphs are presented in Figures 23 and 24. Detailed server utilization can be found in Table 34. Tables 35, 41 and 36 contains respectively applications makespan and sumflow gains, results on different metrics for the independent tasks and average percentage per task gains.

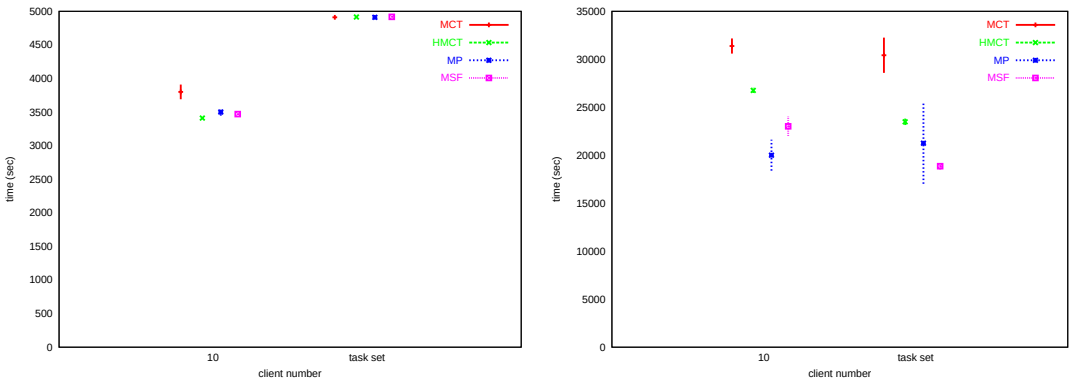

Figure 23. Scenario (h): makespan and sumflow results for the first experiment

Results for HMCT are good and in one way the best we ever had in all the experiments, because for the first time it beats MSF on one metric: the makespan. But, as said previoulsy, some tasks are missing for being rejected by a server that could not undertake it because of a too high load. Consequently these tasks have not interfered with previoulsy and future assigned tasks on the corresponding server. Worst, the submission of the stencil is biased, so the makespan. HMCT results can be seen as ' boosted up'.
We already encounter this situation during dgemm experiment (see section 5.2.1), with both MCT and HMCT heuristics. One must consider that HMCT tries to optimize MCT with the help of HTM information. Indeed, when the agent receives a new query, MCT computes its completion date as if no task would finish during its execution. This can be considered as a '*w*orst case expectation', because tasks can end up, minimizing the new query completion date. HMCT tries to use the server capacity which is not able to accept another request. We do not have mechanisms to limit the number of tasks on a server, which could temperate the 'aggressive' behavior of

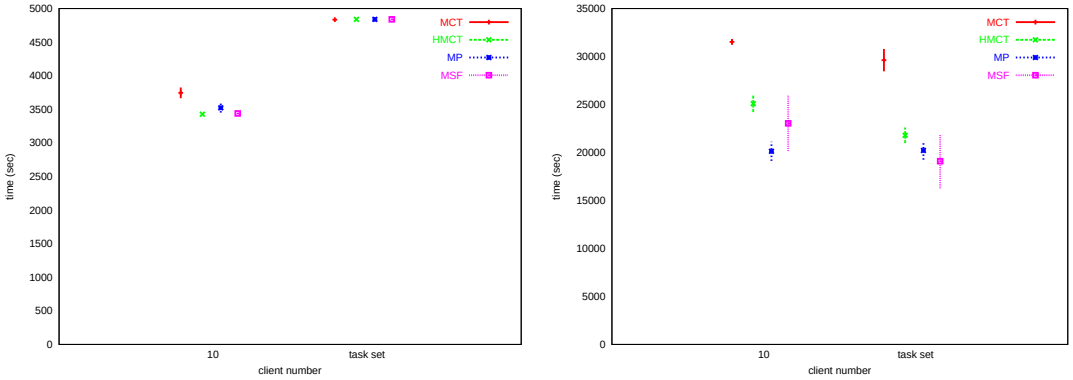

Figure 24. Scenario (h): makespan and sumflow results for the second experiment

server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
experiment 1								
spinnaker	49.1 (32.6 7.1 9.4)	28686	49.4 (33.8 7.3 8.3)	20656	50.7 (37.9 6.1 6.7)	15156	48.7 (33.5 7.3 7.9)	17467
artimon	48.0 (40.3 3.7 4.0)	29052	40.3 (30.3 4.2 5.8)	23460	40.1 (30.4 4.3 5.3)	13735	39.4 (29.1 4.0 6.3)	15904
soyotte	1.6 (0.8 0.4 0.4)	2183	5.0 (4.9 0.0 0.1)	2951	4.6 (3.3 0.5 0.9)	5896	5.8 (5.7 0.1 0.0)	4046
fonck	1.4 (0.6 0.4 0.4)	1890	5.3 (5.3 0.0 0.0)	3179	4.6 (2.7 0.6 1.3)	6475	6.1 (6.0 0.2 0.0)	4462
total sumflow		61811		50246		41262		41879
experiment 2								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	48.7 (33.3 6.7 8.7)	27258	48.8 (34.3 5.7 8.8)	18765	50.6 (38.0 5.4 7.2)	15337	47.4 (32.4 6.7 8.3)	17437
artimon	48.6 (39.7 4.2 4.6)	30012	40.9 (30.0 5.8 5.1)	22099	41.4 (31.4 5.3 4.7)	14384	40.4 (30.0 4.8 5.6)	15988
soyotte	1.0 (0.6 0.2 0.2)	1516	4.7 (4.7 0.0 0.0)	2757	4.0 (2.7 0.4 0.9)	5048	6.1 (6.1 0.0 0.0)	4299
fonck	1.7 (0.9 0.5 0.3)	2364	5.6 (5.6 0.0 0.0)	3265	3.9 (2.4 0.5 1.0)	5566	6.1 (6.0 0.1 0.0)	4409
total sumflow		61150		46886		40335		42133
MEAN								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	48.9 (33.0 6.9 9.0)	27972	49.1 (34.0 6.5 8.5)	19710	50.7 (37.9 5.8 7.0)	15246	48.0 (32.9 7.0 8.1)	17452
artimon	48.3 (40.0 4.0 4.3)	29532	40.6 (30.1 5.0 5.5)	22780	40.8 (30.9 4.8 5.0)	14060	39.9 (29.6 4.4 5.9)	15946
soyotte	1.3 (0.7 0.3 0.3)	1850	4.8 (4.8 0.0 0.0)	2854	4.3 (3.0 0.4 0.9)	5472	6.0 (5.9 0.0 0.0)	4172
fonck	1.5 (0.7 0.4 0.4)	2127	5.5 (5.5 0.0 0.0)	3222	4.2 (2.6 0.6 1.1)	6020	6.1 (6.0 0.1 0.0)	4436
total sumflow		61480		48566		40798		42006

Table 34. Scenario (h): servers utilization

	STENCIL makespan			STENCIL sumflow			METATASK sumflow		
	HMCT	MP	MSF	HMCT	MP	MSF	HMCT	MP	MSF
experiment 1	10.2	7.9	8.7	14.7	36.3	26.7	22.8	30.1	38
experiment 2	8.5	6.0	8.2	20.4	36.2	26.9	25.5	31.4	36.2
MEAN	9.4	6.9	8.4	17.6	36.2	26.8	24.2	30.8	37.1

Table 35. Scenario (h): average percentage gain against MCT on the makespan and the sumflow for each client

HMCT, nor fault tolerance mechanisms (a client message would be needed to return the server ID to the agent), so the request is abandonned by the client.

		mean flow MCT (sec)	gain in percentage HMCT	MP	MSF
	type 1	87.6	14.5	29.3	25.1
experiment 1	type 2	163.0	22.8	28.7	38.0
	type 3	279.1	25.6	31.1	42.4
	type 1	86.0	21.1	37.1	17.1
experiment 2	type 2	187.8	22.5	34.5	36.1
	type 3	250.0	31.0	28.1	42.3
MEAN	-	175.6	22.9	31.5	33.5

Table 36. Scenario (h): average percentage gain for $\mu = 28$ sec on each task given by type

Nonetheless, it is interesting to see that, even with this "time advantage", MP and MSF are still beating HMCT on most of the metric on the average: this seems to confirm that minimizing the finishing completion time of the new query without taking in account the interference with already assigned tasks is maybe not the right policy to undertake in our context.

We must also observe that MP does not give bad results on the makespan of the stencil application. Indeed, it even achieves a 7% gain. Because of independent tasks, we have not the 'synchronization barier' effect like in previous scenarios.

Scenario (i)
This section deals with the same kind of experiment as the one above. Inter-arrival date is drawn from a Poisson distribution with the parameter μ equal here to 40 seconds. 4 seeds have been used to generate the experiments whose compositions are given in Table 37. Each of them have been submitted 6 times.

There are 86 independent tasks launched during the submission of a stencil application. The stencil graph is 10 tasks wide width and 25 depth long. In consequence 336 tasks are submitted to the agent during a run.

	type 1	type 2	type 3
experiment 1	35	19	32
experiment 2	30	24	32
experiment 3	34	28	24
experiment 4	28	28	30

Table 37. Scenario (i): independent tasks composition

One can see in Figures 25, 26, 27 and 28 graphs of the mean and standard deviation of the makespan and the sumflow for stencil and metatask applications. Table 38 presents the cost per server in term of sumflow, the total sumflow cost of the experimentand tasks affectation percentages per server. In Table 39 gains realized on the makespan and on the sumflow for the each client (here the client for the stencil and the client for the set of independent tasks) is given, and finally results on all metrics and quality of service for the independent tasks can be found in Tables 40 and 42.

Firstly, one can observe that we obtain indentical results regardless the figure. On the makespan of the stencil, MSF is the best with a slight advance in front of MP and HMCT. On the sumflow, MP and MSF outperfom the other, MP with a higher standard deviation for the independent tasks and MSF for the stencil graph. Results have then to decide between them.

Table 38 shows a that all heuristics behaves like they are used to unlike with scenarios (f) and (g).

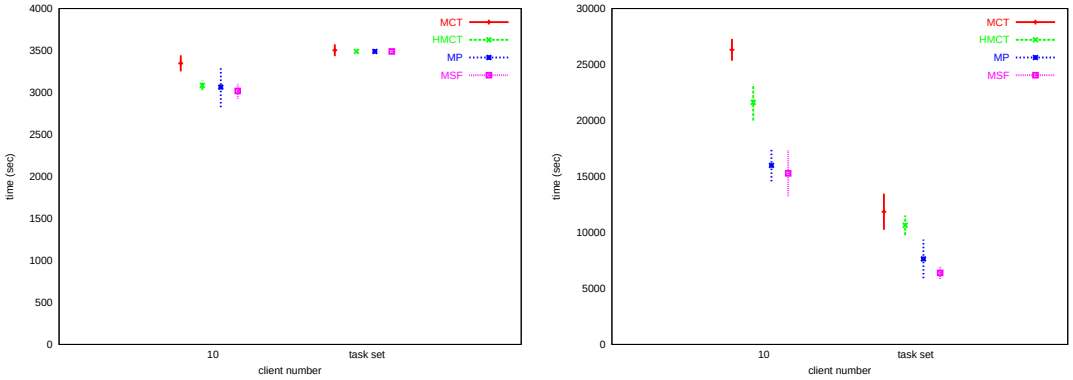

Figure 25. Scenario (i): makespan and sumflow results for the first experiment

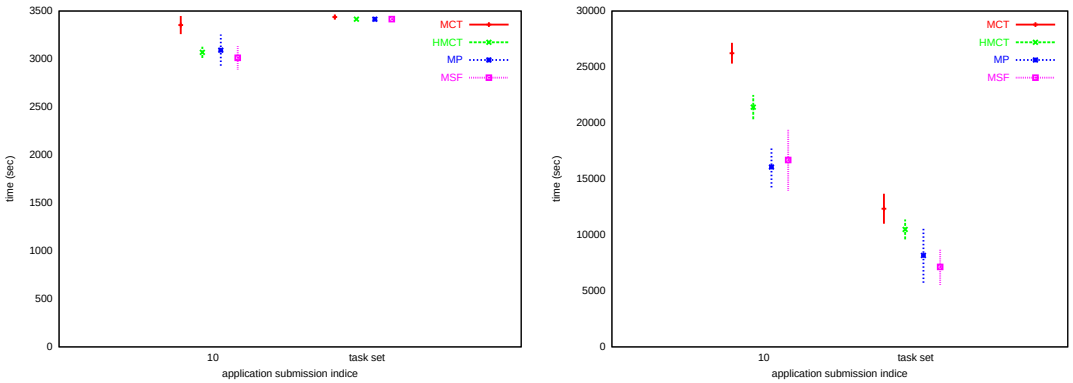

Figure 26. Scenario (i): makespan and sumflow results for the second experiment

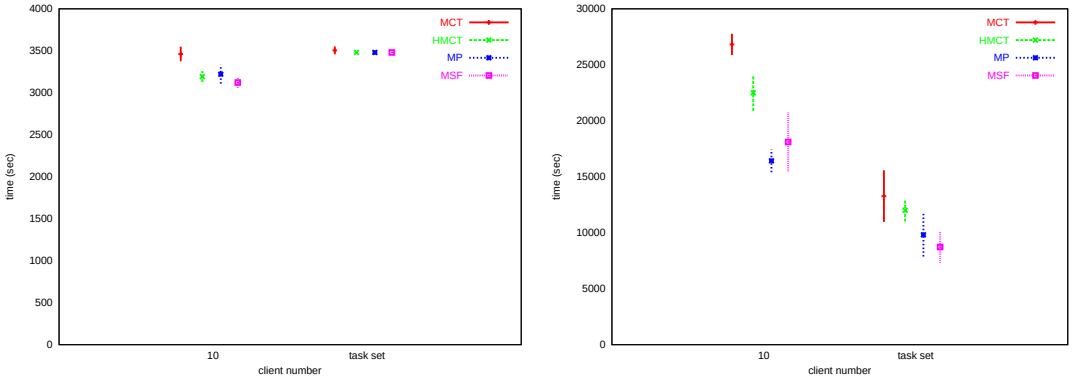

Figure 27. Scenario (i): makespan and sumflow results for the third experiment

MSF behaves the best on most of the metrics: in Table 40, an indepedent task is 38.4% shorter than if scheduled with MCT. MSF achieves a maxstretch equal to the one of HMCT with a lower maxflow and the largest percentage of tasks finishing sooner than MCT with 69%.

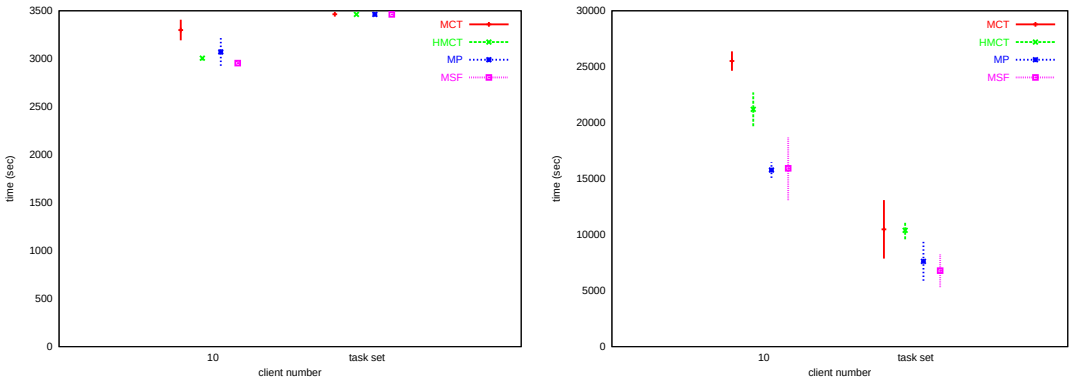

Figure 28. Scenario (i): makespan and sumflow results for the fourth experiment

experiment 1								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	51.8 (41.9 4.2 5.7)	17626	50.9 (41.0 3.9 6.0)	15549	49.6 (40.9 3.9 4.8)	8705	50.3 (40.2 4.4 5.7)	9331
artimon	48.0 (42.6 1.7 3.7)	20277	42.0 (36.4 2.0 3.6)	13640	39.5 (34.0 1.8 3.7)	7669	39.0 (33.6 1.6 3.8)	7664
soyotte	0.1 (0.0 0.0 0.0)	107	3.2 (3.2 0.0 0.0)	1376	5.5 (4.8 0.1 0.5)	3585	4.9 (4.9 0.0 0.0)	2152
fonck	0.1 (0.0 0.0 0.0)	158	3.9 (3.9 0.0 0.0)	1693	5.4 (4.8 0.1 0.5)	3669	5.8 (5.8 0.0 0.0)	2518
total sumflow		38168		32258		23628		21665
experiment 2								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	51.0 (38.8 6.2 6.0)	17041	50.1 (39.6 4.5 6.0)	14763	49.4 (39.8 4.2 5.4)	9102	47.8 (36.8 4.8 6.2)	9796
artimon	49.0 (43.6 2.1 3.2)	21509	42.0 (34.9 3.8 3.3)	13718	39.8 (33.3 3.3 3.2)	7868	40.6 (34.0 3.5 3.0)	8604
soyotte	0.0 (0.0 0.0 0.0)	0	3.8 (3.8 0.0 0.0)	1639	5.4 (4.5 0.6 0.2)	3575	5.7 (5.7 0.0 0.0)	2629
fonck	0.0 (0.0 0.0 0.0)	22	4.1 (4.1 0.0 0.0)	1795	5.4 (4.8 0.2 0.4)	3685	6.0 (6.0 0.0 0.0)	2809
total sumflow		38572		31915		24230		23838
experiment 3								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	52.8 (43.3 3.8 5.7)	21081	50.3 (40.6 4.3 5.4)	16161	50.4 (42.0 3.5 4.9)	10028	47.9 (37.8 4.0 6.1)	11315
artimon	46.8 (39.5 3.2 4.1)	18604	41.4 (34.1 2.8 4.5)	14736	40.1 (33.8 2.7 3.6)	8649	39.8 (32.9 3.2 3.7)	9725
soyotte	0.0 (0.0 0.0 0.0)	0	3.6 (3.6 0.0 0.0)	1570	4.8 (3.6 0.5 0.6)	3647	6.1 (6.1 0.0 0.0)	2831
fonck	0.4 (0.3 0.1 0.0)	406	4.7 (4.7 0.0 0.0)	2046	4.8 (3.6 0.4 0.7)	3921	6.2 (6.2 0.0 0.0)	2963
total sumflow		40091		34513		26245		26834
experiment 4								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	52.1 (42.4 5.3 4.4)	16926	51.2 (42.3 4.8 4.2)	14903	49.5 (41.0 4.7 3.8)	8741	49.6 (40.3 5.0 4.4)	9736
artimon	47.9 (42.1 3.0 2.7)	19045	42.0 (35.4 3.6 3.0)	13737	40.3 (35.0 2.7 2.6)	7590	39.7 (33.6 3.4 2.8)	8367
soyotte	0.0 (0.0 0.0 0.0)	21	2.7 (2.7 0.0 0.0)	1158	5.6 (5.0 0.3 0.2)	3491	5.2 (5.2 0.0 0.0)	2251
fonck	0.0 (0.0 0.0 0.0)	0	4.2 (4.2 0.0 0.0)	1796	4.7 (3.5 0.6 0.5)	3579	5.5 (5.5 0.0 0.0)	2362
total sumflow		35992		31594		23401		22716
MEAN								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	51.9 (41.6 4.9 5.5)	18168	50.6 (40.9 4.4 5.4)	15344	49.7 (40.9 4.1 4.7)	9144	48.9 (38.8 4.5 5.6)	10044
artimon	47.9 (41.9 2.5 3.4)	19859	41.8 (35.2 3.1 3.6)	13958	39.9 (34.0 2.6 3.3)	7944	39.8 (33.5 2.9 3.3)	8590
soyotte	0.0 (0.0 0.0 0.0)	32	3.3 (3.3 0.0 0.0)	1436	5.3 (4.5 0.4 0.4)	3574	5.5 (5.5 0.0 0.0)	2466
fonck	0.2 (0.1 0.0 0.0)	146	4.2 (4.2 0.0 0.0)	1832	5.1 (4.2 0.3 0.5)	3714	5.8 (5.8 0.0 0.0)	2663
total sumflow		38206		32570		24376		23763

Table 38. Scenario (i): processors utilization

	STENCIL						METATASK		
	makespan			sumflow			sumflow		
	HMCT	MP	MSF	HMCT	MP	MSF	HMCT	MP	MSF
experiment 1	7.8	8.5	9.8	17.9	39.2	41.9	10.2	35.5	46.1
experiment 2	8.5	7.8	10.2	18.3	38.8	36.4	14.3	34.1	42.7
experiment 3	7.8	6.9	9.8	16.1	38.8	32.5	10.2	27.2	35.5
experiment 4	8.9	6.9	10.5	16.9	38.2	37.6	2.7	27.3	35.3
MEAN	8.2	7.5	10.1	17.3	38.7	37.1	9.4	31	39.9

Table 39. Scenario (i): average percentage gain against MCT on the makespan and the sumflow for each client

		mean flow	gain in percentage		
		MCT (sec)	HMCT	MP	MSF
	type 1	69.1	0.0	23.6	37.9
experiment 1	type 2	123.7	12.3	39.4	47.6
	type 3	219.6	12.9	38.2	48.3
	type 1	73.0	0.9	27.4	33.0
experiment 2	type 2	135.6	15.8	29.9	43.1
	type 3	212.0	18.6	38.0	44.2
	type 1	76.2	17.2	29.1	29.7
experiment 3	type 2	149.8	16.6	27.9	39.7
	type 3	226.1	3.8	24.2	32.9
	type 1	64.2	-0.2	27.6	31.3
experiment 4	type 2	138.0	7.2	29.5	42.6
	type 3	184.8	-4.2	25.2	30.8
MEAN	-	139.4	8.4	30.0	38.4

Table 40. Scenario (i): average percentage gain for $\mu = 40$ sec on each task given by type

	NetSolve's MCT			HMCT			MP			MSF		
	$seed_1$	$seed_2$	**Avg**	$seed_1$	$seed_2$	**Avg**	$seed_1$	$seed_2$	**Avg**	$seed_1$	$seed_2$	**Avg**
makespan	4911	4835	**4873**	4915	4839	**4877**	4911	4839	**4875**	4917	4839	**4878**
sumflow	30426	29625	**30026**	23485	21793	**22639**	21254	20209	**20732**	18863	19092	**18978**
maxflow	575.5	637.6	**606.5**	399.1	419.9	**409.5**	658.0	608.4	**633.2**	310.7	344.1	**327.4**
maxstretch	19.3	21.8	**20.6**	10.8	10.9	**10.8**	19.0	17.7	**18.3**	15.9	14.7	**15.3**
percentage of tasks that finish sooner than with NetSolve's MCT	-	-	–	61 (30)	61 (26)	**61(28)**	69 (19)	70 (17)	**70(18)**	75 (16)	66 (21)	**70(18)**

Table 41. Scenario (h): results in seconds for $\mu = 28$ sec on wastecpu tasks

	NetSolve's MCT					HMCT					MP					MSF				
	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**
makespan	3504	3437	3505	3464	**3478**	3489	3415	3480	3462	**3462**	3489	3415	3480	3462	**3462**	3489	3415	3480	3462	**3462**
sumflow	11853	12341	13270	10482	**11986**	10643	10496	12012	10392	**10886**	7640	8167	9819	7623	**8312**	6387	7146	8726	6788	**7262**
maxflow	405.5	429.7	401.2	415.1	**412.9**	317.3	286.8	337.8	325.9	**316.9**	463.0	468.7	482.4	457.0	**467.8**	199.3	220.1	274.0	237.7	**232.8**
maxstretch	10.7	10.4	10.1	10.1	**10.3**	8.3	9.5	8.4	8.6	**8.7**	14.3	13.3	14.2	13.2	**13.8**	6.7	9.3	10.8	8.3	**8.8**
percentage of tasks that finish sooner than with MCT	-	-	-	-	–	52 (40)	56 (37)	54 (39)	49 (41)	**53(39)**	67 (25)	69 (25)	67 (26)	60 (30)	**66(26)**	71 (21)	74 (20)	68 (25)	62 (29)	**69(24)**

Table 42. Scenario (i): results in seconds for $\mu = 40$ sec on wastecpu tasks

5.7. Scenario (j): Submission of a 5*25 Stencil Application Concurrently to 87 Independent Tasks at a Low Rate

We consider the submission of a 5*25 stencil application in parallel of 86 independent tasks. The syencil graph is composed of task of type 1 and its width is smaller than in previous scenarios in order to judge the heuristics facing a lower throughput.

Indeed, the inter-arrival date of two independent tasks is drawn from a Poisson distribution with parameter $\mu = 25$ seconds and only 5 tasks are submitted at the beginning of the stencil submission.

Four seeds have been used to generate four instantiations of this scenario. Each of them have been submitted 6 times to the environment composed of the following servers:

- client: zanzibar ;
- agent: xrousse ;
- servers: spinnaker, artimon, soyotte, fonck.

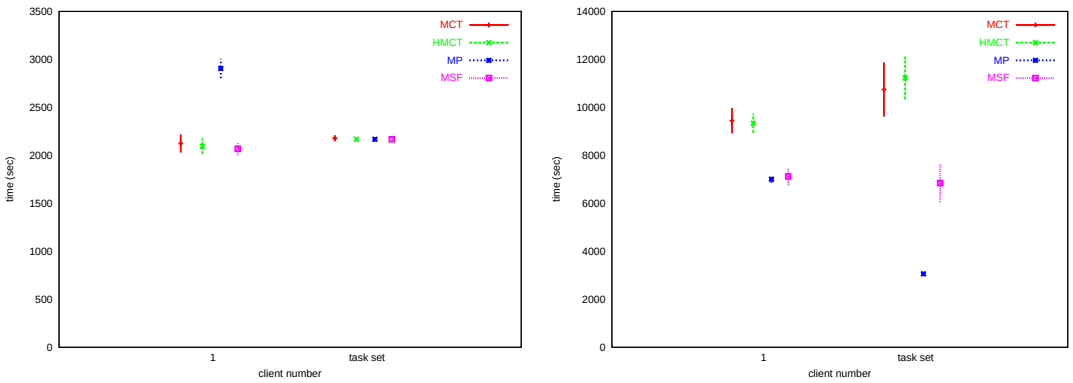

Figure 29. Scenario (j): makespan and sumflow results for the first experiment

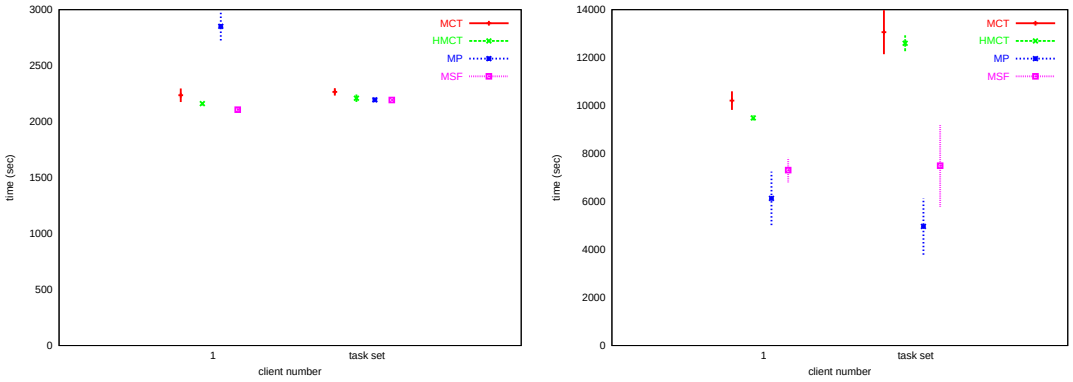

Figure 30. Scenario (j): makespan and sumflow results for the second experiment

Makespan and sumflow results are given in Figures 29, 30, 31 and 32. Servers utilization is given in Table 43 and resulting gains are described in Table 44. Results on the response time is given in Table 45 and an overview of the maxflow, maxtretch metrics as well as the percentage of tasks that finish sooner is provided in Table 46.

The first thing to point out is that MP does not achieve the same result on the makespan than in scenario (g) and (h): it gives the highest makespan, 33.8% higher than the one given by the MCT schedule for the stencil

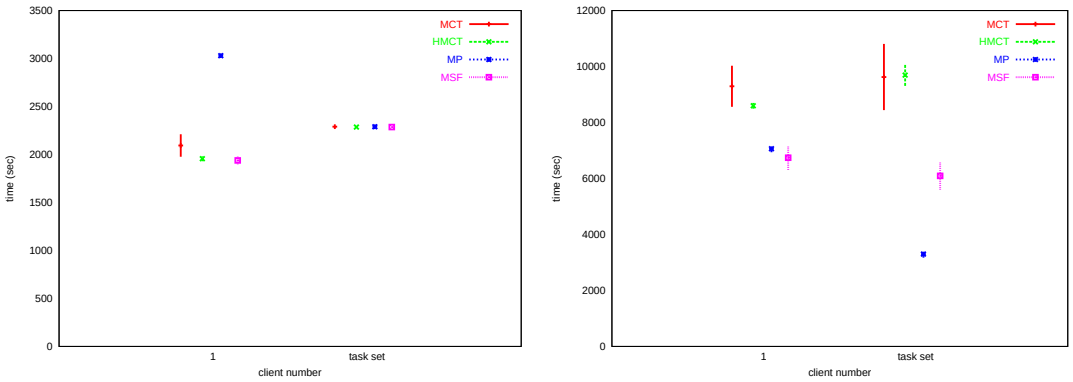

Figure 31. Scenario (j): makespan and sumflow results for the third experiment

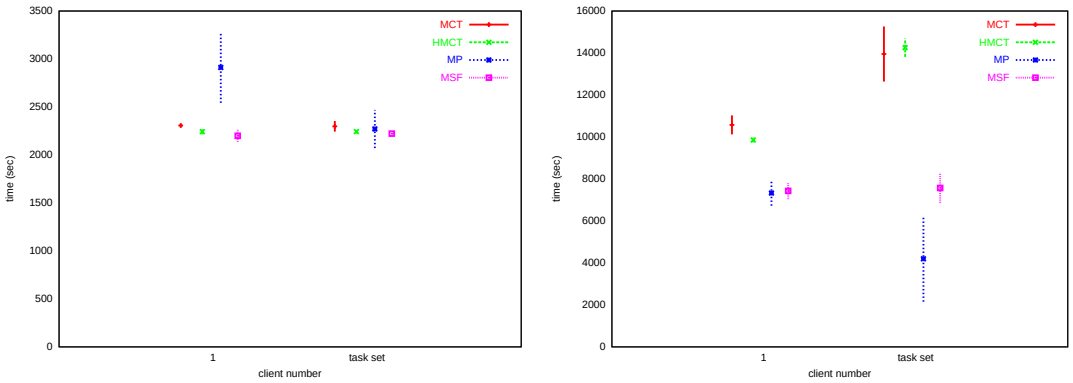

Figure 32. Scenario (j): makespan and sumflow results for the fourth experiment

application. In consequence, MP gives the best performances on the sumflow of the set of independent tasks, the shortest tasks (66.4% shorter than MCT) and 94% of the independent tasks finish sooner than with MCT.

This scenario is very interesting: indeed, one can see that HMCT hardly outperforms MCT. It achieves a 3.5% and 5.6% gain on the makespan and the sumflow respectively of the stencil while some negative performances on the independent tasks: Table 45 shows that a task is 2.2% longer in average when scheduled with HMCT than with MCT and that more tasks finish sooner (50 against 48 for HMCT).

Finally, MSF outperfoms all the other in most of the metrics regardless the client: 5.1% and 27.5% of gain on the makespan and the sumflow of the stencil application and 40% on the sumflow of the set of independent tasks. It minimizes the maxstretch. To sump up, a task scheduled with MSF has 82% of chance to finish sooner then with MCT and is 39% shorter.

experiment 1								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	53.8 (40.9 6.8 6.2)	10480	52.0 (39.7 5.3 7.0)	10195	46.4 (33.1 6.3 7.1)	2729	49.4 (36.7 5.5 7.2)	5990
artimon	46.2 (35.5 5.0 5.7)	9709	45.8 (34.4 6.5 4.8)	9775	34.6 (24.3 5.6 4.7)	2209	43.3 (32.3 6.4 4.6)	6001
soyotte	0.0 (0.0 0.0 0.0)	0	0.6 (0.6 0.0 0.0)	155	8.4 (8.4 0.0 0.0)	2286	2.7 (2.7 0.0 0.0)	721
fonck	0.0 (0.0 0.0 0.0)	0	1.6 (1.6 0.0 0.0)	437	10.5 (10.5 0.0 0.0)	2843	4.6 (4.6 0.0 0.0)	1258
total sumflow		20189		20562		10067		13970
experiment 2								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	53.2 (38.9 6.4 8.0)	12285	52.0 (37.7 6.4 7.9)	10774	44.9 (29.6 7.2 8.2)	3078	49.4 (35.1 7.1 7.2)	6592
artimon	46.8 (34.6 6.0 6.3)	10986	46.2 (33.9 5.9 6.4)	10827	38.5 (29.0 4.0 5.5)	2735	42.3 (30.0 5.2 7.0)	5955
soyotte	0.0 (0.0 0.0 0.0)	0	0.3 (0.3 0.0 0.0)	78	7.1 (6.0 0.9 0.3)	2403	3.2 (3.2 0.0 0.0)	876
fonck	0.0 (0.0 0.0 0.0)	0	1.5 (1.5 0.0 0.0)	411	9.5 (8.9 0.3 0.3)	2884	5.1 (5.1 0.0 0.0)	1386
total sumflow		23271		22090		11100		14809
experiment 3								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	53.9 (39.4 8.6 5.9)	9898	51.3 (35.6 9.4 6.3)	8754	44.1 (28.2 9.2 6.7)	2660	50.0 (35.3 8.8 5.9)	5722
artimon	46.1 (34.0 7.5 4.5)	9020	47.0 (36.1 6.7 4.2)	9074	36.2 (26.0 6.5 3.7)	2241	43.3 (31.5 7.3 4.5)	5288
soyotte	0.0 (0.0 0.0 0.0)	0	0.4 (0.4 0.0 0.0)	104	8.8 (8.4 0.4 0.0)	2513	2.7 (2.7 0.0 0.0)	721
fonck	0.0 (0.0 0.0 0.0)	0	1.3 (1.3 0.0 0.0)	361	10.9 (10.9 0.0 0.0)	2947	4.1 (4.1 0.0 0.0)	1105
total sumflow		18918		18293		10361		12836
experiment 4								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	53.2 (36.8 7.8 8.6)	12972	51.7 (35.5 7.7 8.4)	11810	45.4 (29.7 7.8 8.0)	3296	49.2 (33.8 7.7 7.7)	6354
artimon	46.8 (33.4 6.9 6.5)	11557	45.4 (31.7 7.0 6.7)	11503	35.3 (21.7 6.6 6.9)	2723	41.0 (26.5 7.0 7.5)	6003
soyotte	0.0 (0.0 0.0 0.0)	0	0.5 (0.5 0.0 0.0)	130	9.0 (8.6 0.2 0.2)	2609	4.0 (4.0 0.0 0.0)	1081
fonck	0.0 (0.0 0.0 0.0)	0	2.5 (2.5 0.0 0.0)	669	10.3 (10.1 0.1 0.1)	2895	5.8 (5.8 0.0 0.0)	1565
total sumflow		24529		24112		11523		15003
MEAN								
server	MCT		HMCT		MP		MSF	
	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow	% of tasks	sumflow
spinnaker	53.5 (39.0 7.4 7.2)	11409	51.8 (37.2 7.2 7.4)	10383	45.2 (30.1 7.6 7.5)	2941	49.5 (35.2 7.3 7.0)	6164
artimon	46.5 (34.4 6.4 5.8)	10318	46.1 (34.0 6.5 5.5)	10295	36.1 (25.2 5.7 5.2)	2477	42.5 (30.1 6.5 5.9)	5812
soyotte	0.0 (0.0 0.0 0.0)	0	0.4 (0.4 0.0 0.0)	117	8.3 (7.9 0.4 0.1)	2453	3.1 (3.1 0.0 0.0)	850
fonck	0.0 (0.0 0.0 0.0)	0	1.7 (1.7 0.0 0.0)	470	10.3 (10.1 0.1 0.1)	2892	4.9 (4.9 0.0 0.0)	1328
total sumflow		21727		21264		10763		14154

Table 43. Scenario (j): processors utilization

	STENCIL						METATASK		
	makespan			sumflow			sumflow		
	HMCT	MP	MSF	HMCT	MP	MSF	HMCT	MP	MSF
experiment 1	1.4	-36.8	2.6	1.1	25.8	24.6	-4.5	71.5	36.3
experiment 2	3.4	-27.5	5.8	7.1	39.9	28.4	2.4	63.3	41.7
experiment 3	6.6	-44.7	7.4	7.5	24.0	27.4	0	65.2	37.9
experiment 4	2.8	-26.2	4.6	6.8	30.7	29.7	-1.8	69.2	44.5
MEAN	3.5	-33.8	5.1	5.6	30.1	27.5	-1	67.3	40.1

Table 44. Scenario (j): average percentage gain against MCT on the makespan and the sumflow for each client

		mean flow	gain in percentage		
		MCT (sec)	HMCT	MP	MSF
	type 1	65.1	-7.1	69.1	35.0
experiment 1	type 2	136.4	-1.5	71.9	35.2
	type 3	199.6	-5.3	72.4	37.6
	type 1	77.7	-0.5	55.5	41.7
experiment 2	type 2	149.8	4.0	57.9	43.8
	type 3	227.9	4.6	66.6	42.2
	type 1	55.4	-26.8	59.8	17.4
experiment 3	type 2	117.3	2.8	62.5	37.8
	type 3	180.7	6.7	71.4	43.7
	type 1	79.1	-0.4	70.1	39.8
experiment 4	type 2	149.9	3.3	68.4	49.5
	type 3	233.9	-6.0	70.8	44.8
MEAN	-	139.4	-2.2	66.4	39.0

Table 45. Scenario (j): average percentage gain for $\mu = 25$ sec on each task given by type

	NetSolve's MCT					HMCT					MP					MSF				
	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**	$seed_1$	$seed_2$	$seed_3$	$seed_4$	**Avg**
makespan	2179	2266	2290	2298	**2258**	2168	2209	2286	2244	**2227**	2167	2194	2289	2271	**2230**	2167	2193	2286	2223	**2217**
sumflow	10745	13062	9625	13952	**11846**	11225	12601	9695	14253	**11944**	3060	4965	3299	4195	**3880**	6847	7498	6092	7571	**7002**
maxflow	312.7	332.4	325.3	371.4	**335.5**	270.6	314.1	266.6	321.1	**293.1**	90.2	348.4	231.6	220.5	**222.7**	196.7	203.9	174.9	188.0	**190.8**
maxstretch	8.0	8.4	8.9	9.6	**8.7**	8.4	7.7	8.3	8.0	**8.1**	2.9	11.2	8.1	5.4	**6.9**	8.0	6.4	8.7	7.9	**7.8**
percentage of tasks that finish sooner than with NetSolve's MCT	-	-	-	-	–	44 (54)	54 (44)	46 (52)	47 (52)	**48**(**50**)	97 (2)	90 (10)	91 (6)	97 (3)	**94**(**5**)	78 (20)	89 (10)	71 (25)	89 (10)	**82**(**16**)

Table 46. Scenario (j): results in seconds for $\mu = 25$ sec on wastecpu tasks

5.8. Notes on Heuristics

MCT is the heuristic used by default in NetSolve [CD96]. In fact, it is the only proposed heuristic because it is considered as one of the easiest to implement and one of the best on the makespan metric (note that in [MAS+99], they study it in a space-share context).
We use in this work a platform that has an heterogeneity coefficient (Section 5.1) of at least 6, but 8.9 in the majority of the experiments exposed. On the platform corresponding to this last coefficient, e.g. spinnaker, artimon, fonck and soyotte (Table 3), MCT never really uses the 2 slower servers by itself: when they are used, then, for the main part, it is consequent of the reject of the submission by all overloaded servers that were sorted before in the list given to the client. So it is only thankful to the client error management that MCT may face such an heterogeneity. Consequently, scheduling decisions have disastrous consequences on applications performances as well as on system integrity.
Other remarks are presented below, because they are common with HMCT behavior, and are even easier to explain there.

Historical-MCT relies on both MCT policy and the Historical Trace Manager (Section 2.3). This heuristic can be seen as a 'perfect' time-share MCT, because it has *a priori* a more accurate information on the system state. We use it to judge the pertinence of the idea to minimize the completion time of the last submitted task as regard to the observed metrics. Nevertheless, results show that this policy is not the best even in a mono-client environment (see Scenarios (f) and (g)) and not only on the makespan. Moreover, HMCT tends to overload a server which leads to the incapacity to handle all the submissions in some scenarios.

HMCT is better than MCT, but is well outperformed compared against MP and MSF which have constantly good results regardless the metric, the environment, the number of clients or tasks in the system.

MP uses only the perturbation to compute where to map a new request. Consequently it uses more the slowest servers for tasks of long duration because that kind of task generates more perturbations on a fast and loaded server. On the opposite, MSF uses the simulated duration and then, as long tasks are even longer on slow servers, the schedule generally tends to use slow servers for shorter tasks. These behaviors are confirmed by the results.

MP is better with contention: it gives the best results when the submission throughput is really high for the environment. We have pointed out a drawback that has been showed with Scenarios (f) and (g) for mono-client experiments. As soon as independent tasks are also involved, it can disappear (Scenarios (h) and (i)) or turn to an advantage on other metrics (Scenario (j)).

MSF achieves great performances regardless the metric or the scenario. It gives a good makespan to each client, and good quality of service to independent tasks. It mixes HMCT and MP advantages without their respective drawbacks.

6. Improvements and Future Work

One of the first improvement to implement is the task feedback. There is three ways doing so. Indeed, it can be considered that the job to inform the agent is the server's, or the client's or both. If the last one is used, then network measures can also be computed.

In current NetSolve code, servers send load reports and finishing task messages to the agent. Nevertheless we need to know in our work which task has been terminated on the server. In order to know this, the agent must assign a unique number to each task and this *IDentification* must be known by the agent of course, but also by the client or both the client and the server.

At current time, this work is done and also used in NetSolve and in the VisPerf monitor [3] to have more precise information. The HTM has to change some cost values and the adjustment is taken into account for the next submission, during the scheduling decision, when it gives information to the heuristic.

The completion feedback let to consider:

[3] http://icl.cs.utk.edu/netsolvedev/applications/visperf.html

- It can be used to store the exact duration of some determinist tasks that have been executed on the environment. This can next be used to compute an interpolation of the complexity polynomial, and then more precise expectations of the duration of that class of tasks ;
- The memory management may be a mean to forbid expensive swap exchanges (which are not taken into account in our heuristics) and limit the number of jobs on a server. Nonetheless, this should not be seen as a palliative to the HMCT drawback, because like most of experiments show, servers may even collapse with only computing intensive tasks ;
- Job Cancellation is not feasible in the current state of our work, but seems an *a priori* direct algorithm to code ;
- Even if computing intensive tasks are intrusive in a user system, the heuristic has to manage non-dedicated platforms. For this work, information coming from the /proc directory on Unix server can also be helpful.

These improvements let us envisage other heuristics, some relying on a tradeoff between load and memory consumption.

Moreover, further works has to be done to implement the HTM and the heuristics in DIET [CDF+01], a french Problem Solving Environment built on top of a hierarchical agent structure.

7. Conclusions

We have examined the behavior of four heuristics Minimum Completion Time, Historical MCT, Minimum Perturbation and Minimum Sumflow facing numerous different scenarios of submission in real environments. Some scenarios, like Scenarios (a) and (b), involve only independent tasks. Others involve 1D-mesh or stencil applications like Scenarios (c), (d), (f) et (g). Scenarios (e), (h), (i) and (j) mix the two kinds. The experimentations, if extensive, cannot be exhaustive: there are an infinity of possible variants that would require too many time. Our work already represents more than 50 days of non-stop running. Nonetheless, we believe that our results are significant to validate the HTM and our heuristics.

We have compared our heuristics HMCT, MP and MSF against MCT, a widely used scheduling heuristic and the default in NetSolve, a Problem Solving Environment. They rely on a prediction module called the Historical Trace Manager. The HTM simulates the execution of all the tasks on the environment and give according information on the duration of any task that has been submitted. These information can be exploited to try to minimize other metric than the common makespan at the same time.

For this work, the HTM and the heuristics have been integrated in the code of NetSolve. The distributed heterogeneous servers used for our experiments were dedicated to the environment, but the network is the laboratory's.

Our work shows that MCT, with load correction mechanisms, do not achieve to perform well in a time-share environment of heterogeneity coefficient of at least 6. HMCT gives much better results in average. This validates the HTM approach because HMCT and MCT rely on the same policy: to finish the last request the soonest in order to minimize the overall makespan.

Nevertheless locally optimizing the makespan may not be the best policy: tasks that have been scheduled for some reason on a server can be delayed by future request(s). With the HTM information, heuristics can consider the perturbation tasks have on each other. This have the two following consequences: a better accuracy on the system state and the possiblity to exploit at best the available resources for the new task without penalizing still running tasks. This gives a higher quality of service to each client.

Results show that HMCT, MP and MSF, specifically designed for heterogeneous environment where there is a high probablity of perturbation, outperform MCT. MSF appears to be the best averall heuristics as it always outperforms MCT on all criteria.

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